

Tests of fundamental symmetries with atmospheric neutrinos

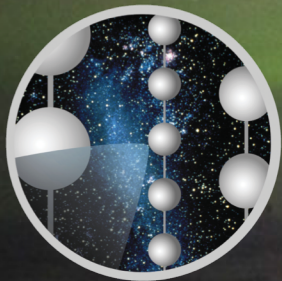
Tom Stuttard

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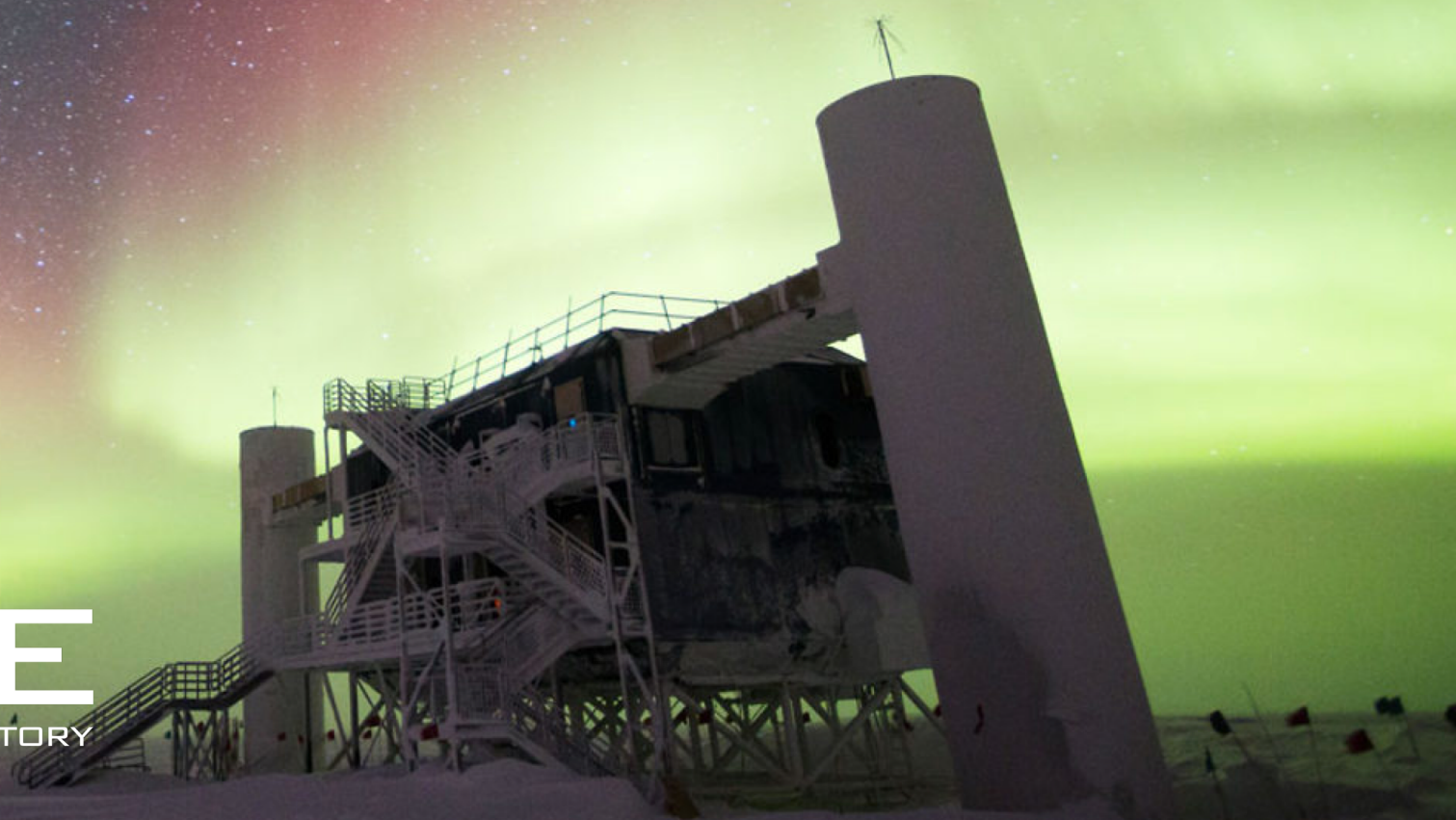
IceDUNE 2021

CARLSBERG FOUNDATION

VILLUM FONDEN

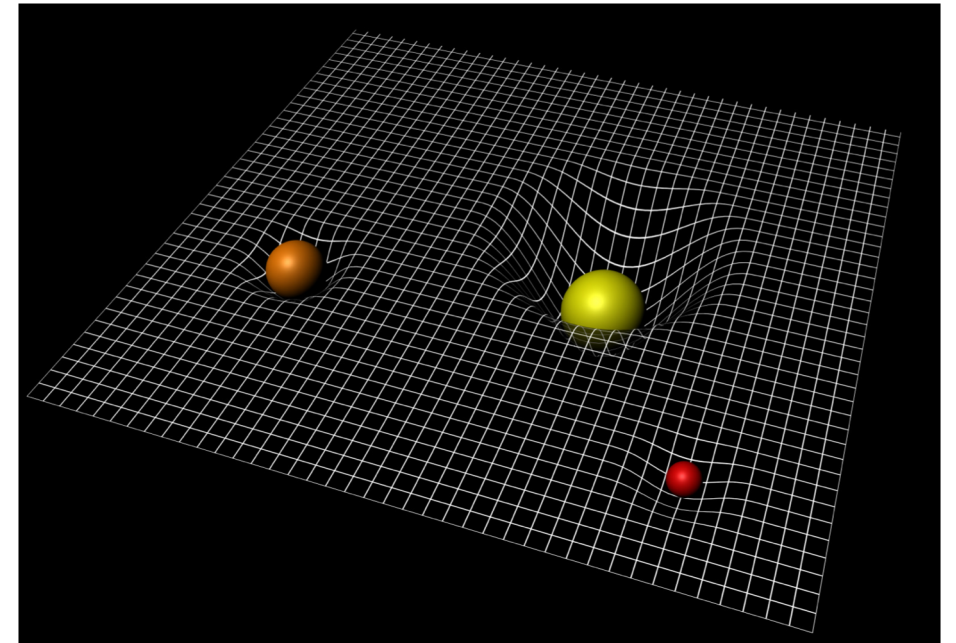


ICECUBE
SOUTH POLE NEUTRINO OBSERVATORY



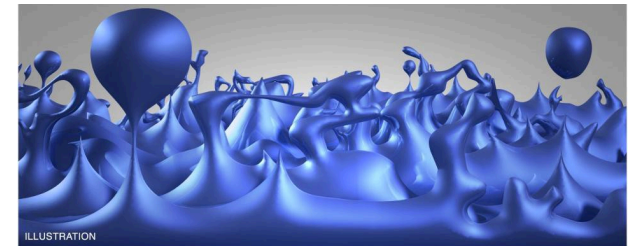
The fundamental properties of Nature as we know it

- Our current understanding of the Universe (SM + GR) features various symmetries/rules
 - Lorentz invariance
 - CPT symmetry
 - Equivalence principal
- Space-time is boring
 - Smooth and stable
 - Microscopically flat far from massive objects
- Evolution of quantum states is boring
 - Deterministic, reversible and unitary in empty space



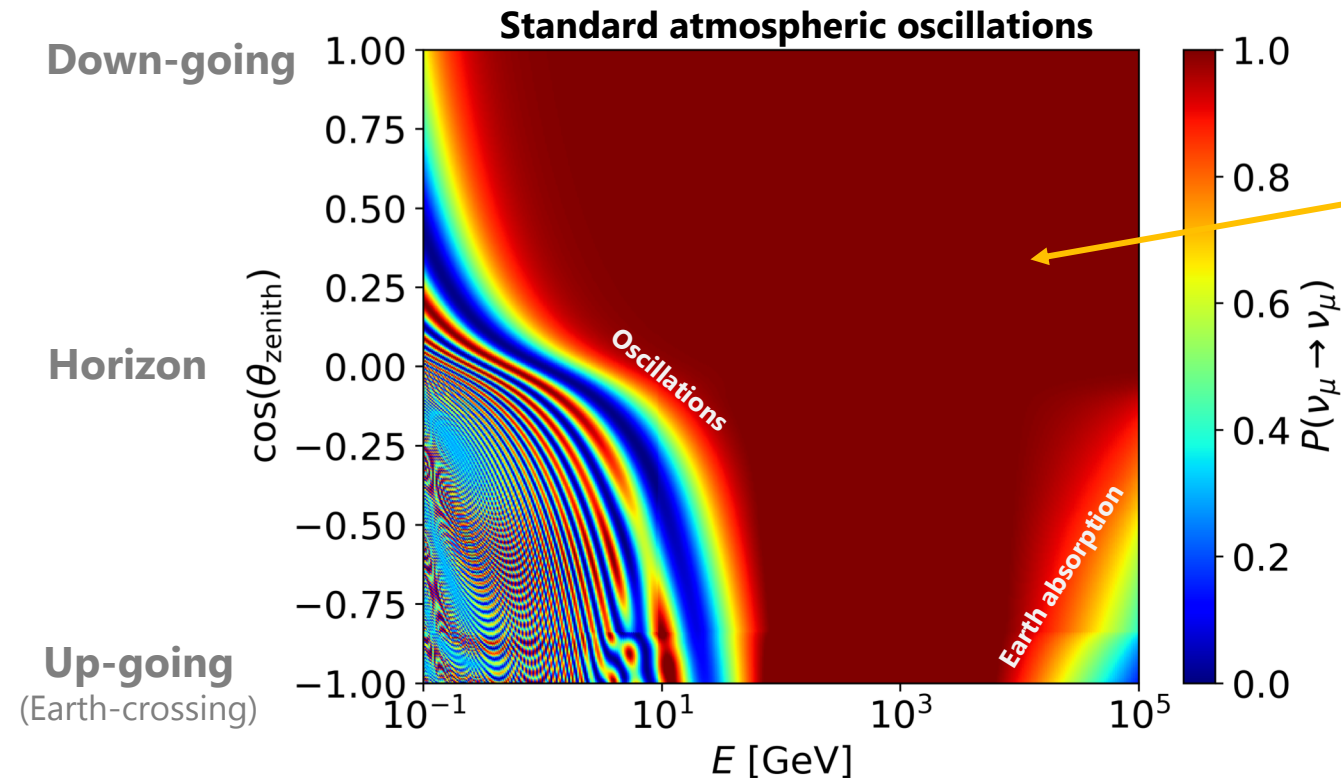
Physics at high energy scales

- New **high energy theories** proposed to solve shortcomings of the SM/GR
 - e.g. **quantum gravity** (QG)
 - $E \sim 10^{19}$ GeV, $L \sim 10^{-35}$ m (the **Planck scale**)
- SM is then a low energy limit of this new theory
- **Modifications of space-time** and **violations of fundamental properties/symmetries** often predicted in such high energy theories
 - These effects are suppressed at the “low” energies we observe
- Searching for these effects requires:
 - High energies \rightarrow overcome suppression
 - Precision \rightarrow effects are small
 - Large travel distances \rightarrow accumulation of tiny effects of space-time defects



Atmospheric neutrino oscillations

- Neutrinos act as tiny quantum interferometers
 - Modifications to space-time interferes with superposition producing oscillations
- The high energies/baselines and copious, well understood flux of atmospheric neutrinos is a powerful testing ground for such effects



**Any $\gtrsim 100$ GeV oscillations
= new physics!**

(especially ν_{τ})

**$\mathcal{O}(1 - 10)$ mHz rates for
IceCube (Upgrade)**

Lorentz invariance violation

Lorentz invariance violation (LIV)

- **Lorentz invariance** - *Experimental results are independent of the orientation and velocity of the laboratory frame*
- LIV frequently predicted by high energy/GUT theories, e.g. quantum gravity, string theory, SUSY, ...
 - LIV suppressed at energy scales we can currently access
- Example phenomenology:
 - Energy-dependent speed of light (modified dispersion relation)
 - Preferred direction of space-time

Standard Model Extension (SME)

- Effective field theory extending the SM to include all possible Lorentz invariance violating operators
 - Features both CPT preserving and violating operators

- Example neutrino Hamiltonian in SME:

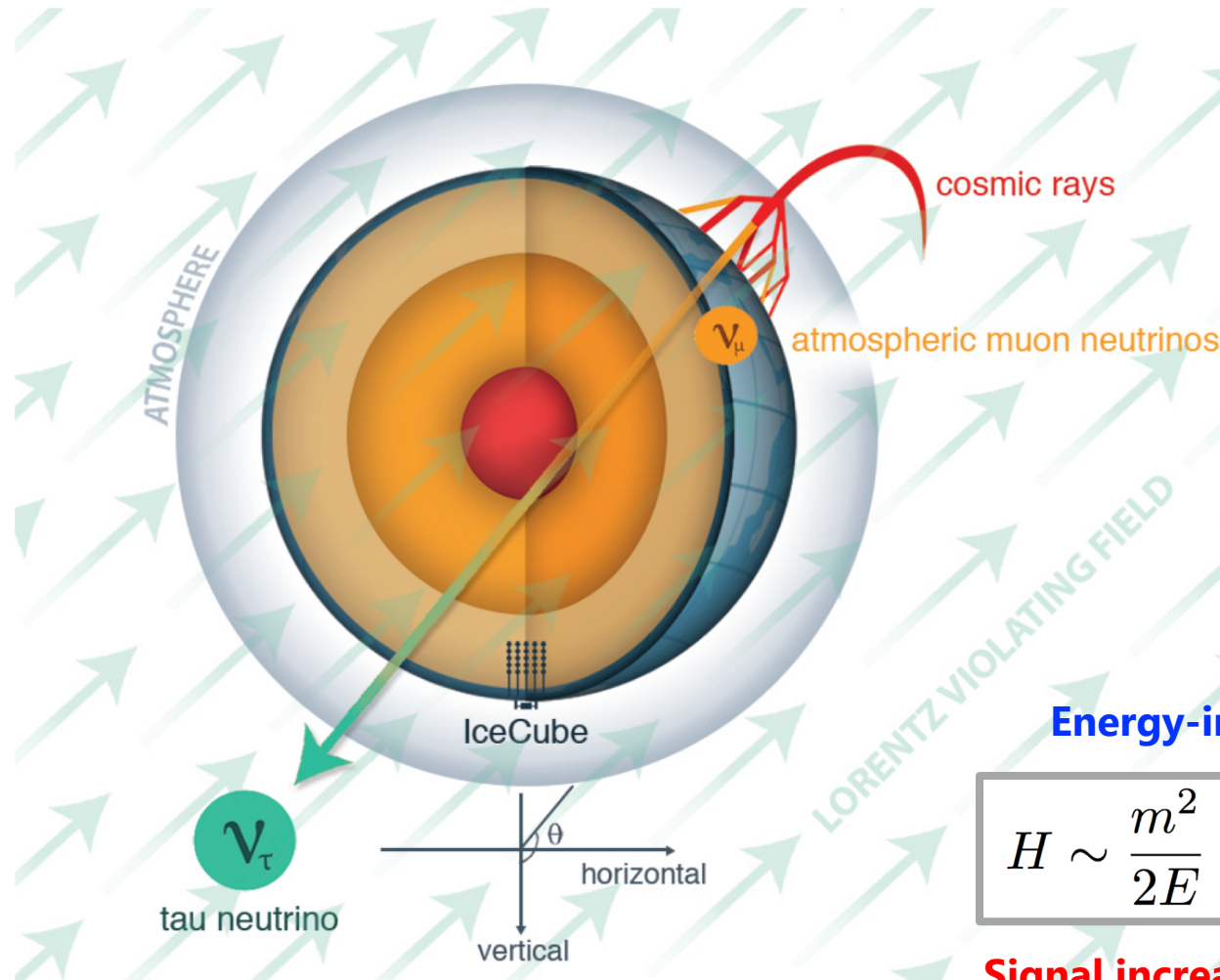
$$H \sim \underbrace{\frac{m^2}{2E}}_{\text{Standard oscillations}} + \underbrace{\overset{\circ}{a}^{(3)} - E \cdot \overset{\circ}{c}^{(4)} + E^2 \cdot \overset{\circ}{a}^{(5)} - E^3 \cdot \overset{\circ}{c}^{(6)} \dots}_{\text{LIV operators}}$$

a = CPT odd
c = CPT even

- Many SME tests performed
 - Neutrino oscillations, accelerator, γ -ray, CRs, CMB, precision nuclear/atomic lab tests, ...

Atmospheric neutrino tests

- Atmospheric neutrino flavour transitions modified by a LIV field



Signal is anomalous $\nu_\mu \rightarrow \nu_\tau$ transitions
 (Only prompt and astrophysical ν_τ expected above 100 GeV in vSM)

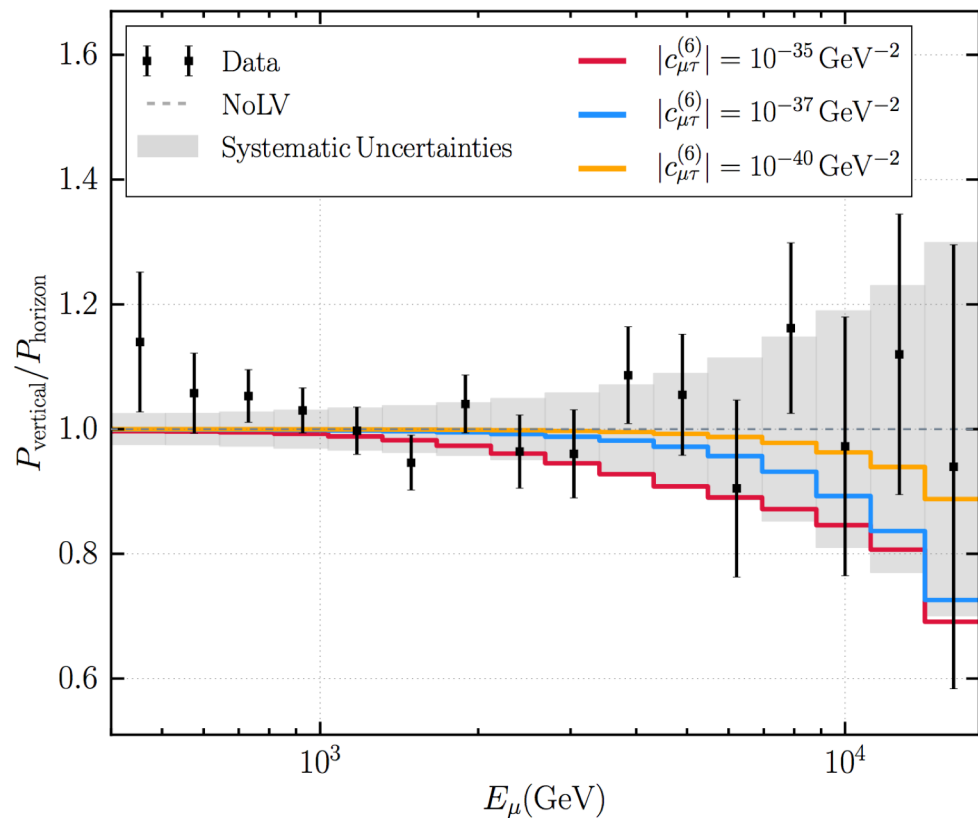
Energy-independent signal for lowest order operator

$$H \sim \frac{m^2}{2E} + \boxed{\dot{a}^{(3)}} - \boxed{E \cdot \dot{c}^{(4)} + E^2 \cdot \dot{a}^{(5)} - E^3 \cdot \dot{c}^{(6)} \dots}$$

Signal increases with energy for all higher order operators

Atmospheric neutrino tests

- IceCube atmospheric neutrino LIV tests performed with 2 years of data
 - World's most stringent constraints on higher order SME operators

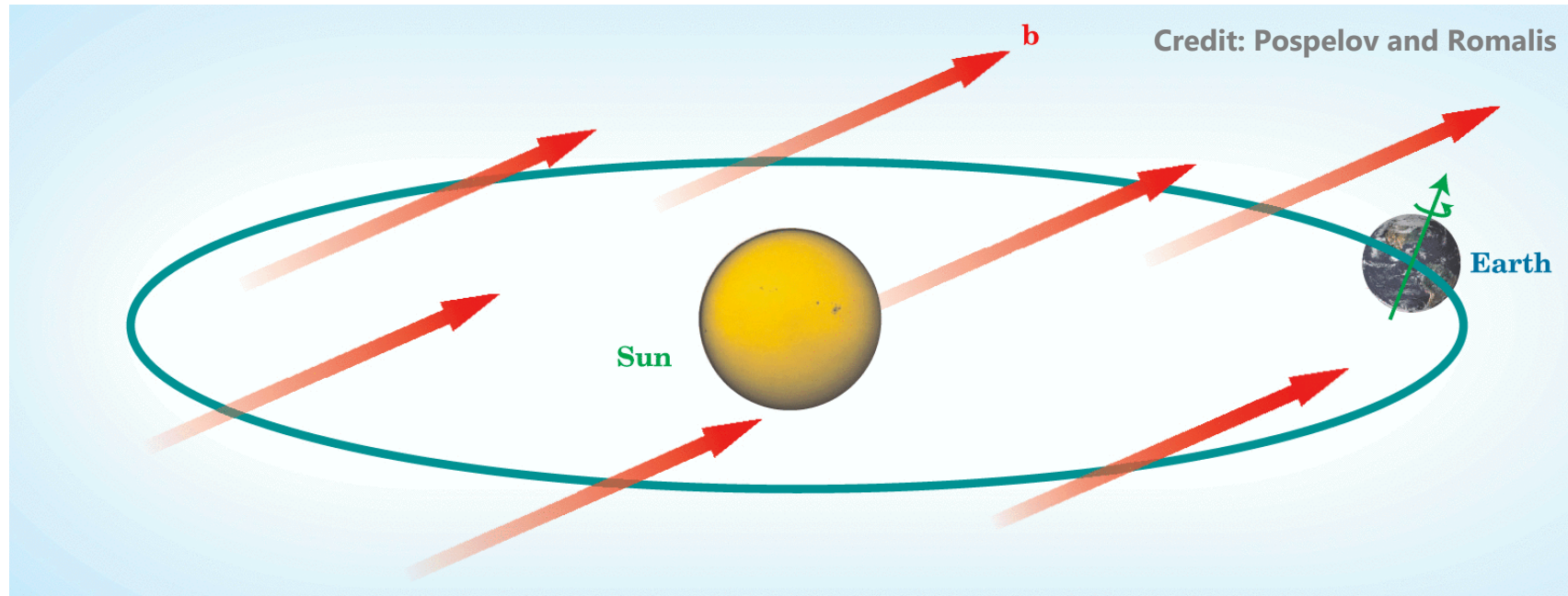


dim.	method	type	sector	limits	ref.
3	CMB polarization	astrophysical	photon	$\sim 10^{-43}$ GeV	[5]
	He-Xe comagnetometer	tabletop	neutron	$\sim 10^{-34}$ GeV	[10]
	torsion pendulum	tabletop	electron	$\sim 10^{-31}$ GeV	[12]
	muon g-2	accelerator	muon	$\sim 10^{-24}$ GeV	[13]
	neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{a}_{\mu\tau}^{(3)}) , \text{Im}(\hat{a}_{\mu\tau}^{(3)}) < 2.9 \times 10^{-24}$ GeV (99% C.L.) $< 2.0 \times 10^{-24}$ GeV (90% C.L.)	this work
4	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-38}$	[6]
	Laser interferometer	LIGO	photon	$\sim 10^{-22}$	[7]
	Sapphire cavity oscillator	tabletop	photon	$\sim 10^{-18}$	[8]
	Ne-Rb-K comagnetometer	tabletop	neutron	$\sim 10^{-29}$	[11]
	trapped Ca ⁺ ion	tabletop	electron	$\sim 10^{-19}$	[14]
neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{c}_{\mu\tau}^{(4)}) , \text{Im}(\hat{c}_{\mu\tau}^{(4)}) < 3.9 \times 10^{-28}$ (99% C.L.) $< 2.7 \times 10^{-28}$ (90% C.L.)	this work	
5	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-34}$ GeV ⁻¹	[6]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-22}$ to 10^{-18} GeV ⁻¹	[9]
	neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{a}_{\mu\tau}^{(5)}) , \text{Im}(\hat{a}_{\mu\tau}^{(5)}) < 2.3 \times 10^{-32}$ GeV ⁻¹ (99% C.L.) $< 1.5 \times 10^{-32}$ GeV ⁻¹ (90% C.L.)	this work
6	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-31}$ GeV ⁻²	[6]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-42}$ to 10^{-35} GeV ⁻²	[9]
	gravitational Cherenkov radiation	astrophysical	gravity	$\sim 10^{-31}$ GeV ⁻²	[15]
	neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{c}_{\mu\tau}^{(6)}) , \text{Im}(\hat{c}_{\mu\tau}^{(6)}) < 1.5 \times 10^{-36}$ GeV ⁻² (99% C.L.) $< 9.1 \times 10^{-37}$ GeV ⁻² (90% C.L.)	this work
7	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-28}$ GeV ⁻³	[6]
	neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{a}_{\mu\tau}^{(7)}) , \text{Im}(\hat{a}_{\mu\tau}^{(7)}) < 8.3 \times 10^{-41}$ GeV ⁻³ (99% C.L.) $< 3.6 \times 10^{-41}$ GeV ⁻³ (90% C.L.)	this work
8	gravitational Cherenkov radiation	astrophysical	gravity	$\sim 10^{-46}$ GeV ⁻⁴	[15]
	neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{c}_{\mu\tau}^{(8)}) , \text{Im}(\hat{c}_{\mu\tau}^{(8)}) < 5.2 \times 10^{-45}$ GeV ⁻⁴ (99% C.L.) $< 1.4 \times 10^{-45}$ GeV ⁻⁴ (90% C.L.)	this work

- SuperK results too, and new 8+ year IceCube measurement on the way

Sidereal effects

- LIV may result in preferred direction of Universe
 - Terrestrial physics would then depend on current orientation of Earth w.r.t. this direction
 - Expect sidereal variation in atmospheric neutrino flavour transitions



- Old (2010) IceCube search (PhysRevD.82.112003), not revisited since
- Synergy in testing with spatially separated detectors (e.g. IceCube + DUNE)

CPT violation

CPT violation (CPT-V)

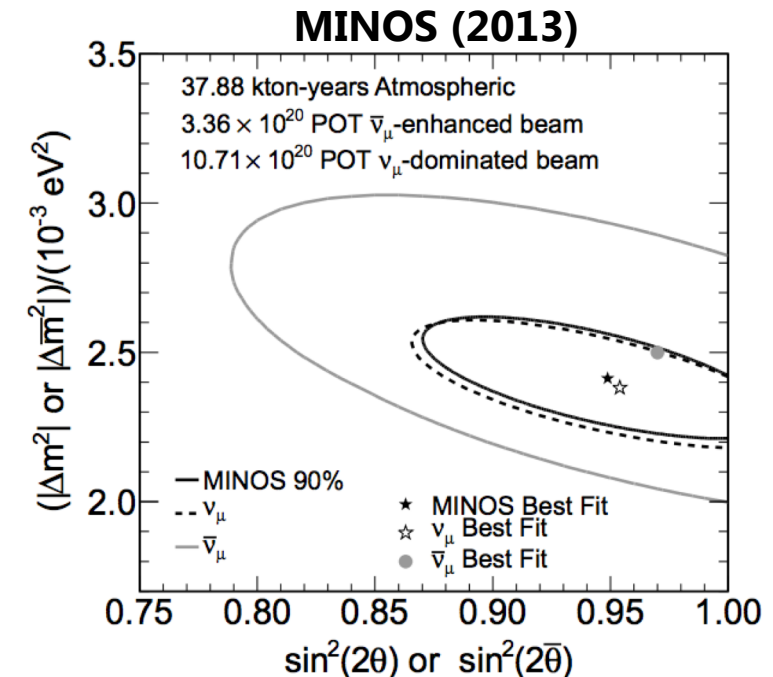
- **CPT symmetry** – *Physics is unchanged under combined C (charge), P (parity) and T (time) transformations*
 - CPT proven to hold in a local quantum field theory, if:
 - It is unitary
 - Lorentz invariance holds
 - Space-time is flat
- All potentially violated by quantum gravity → CPT violation?**
- Information loss in virtual black holes*
- LIV*
- Fluctuating space-time metric*
- Phenomenology: Differing particle vs antiparticle properties
 - e.g. mass, lifetime, ...
-
- A diagram illustrating the relationship between CPT symmetry conditions and quantum gravity. A red bracket groups the three conditions: 'It is unitary', 'Lorentz invariance holds', and 'Space-time is flat'. A red arrow points from this bracket to the text 'All potentially violated by quantum gravity → CPT violation?'. Three grey arrows originate from this text: one points to 'It is unitary' (labeled 'LIV'), one points to 'Lorentz invariance holds' (labeled 'Information loss in virtual black holes'), and one points to 'Space-time is flat' (labeled 'Fluctuating space-time metric').

CPT violation in neutrinos

- CPT-V could produce differing neutrino vs antineutrino mixing angles and/or mass splittings

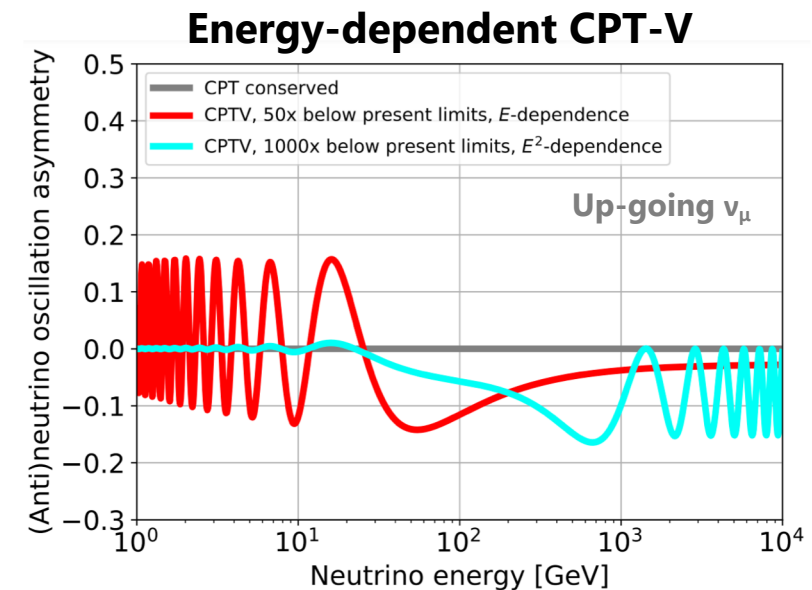


- Neutrino oscillations sensitive to very small ($\ll eV$) mass differences
→ excellent CPT-V search channel
- Searches with [SuperK](#), [MINOS](#) and [global data](#)
 - Sensitivity studies for [DUNE](#), [HyperK](#) and [ESSnuSB](#)



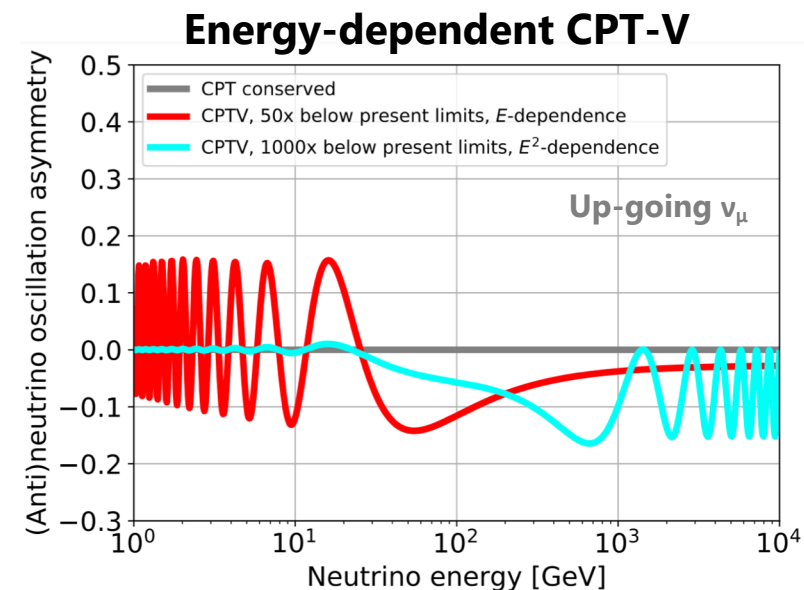
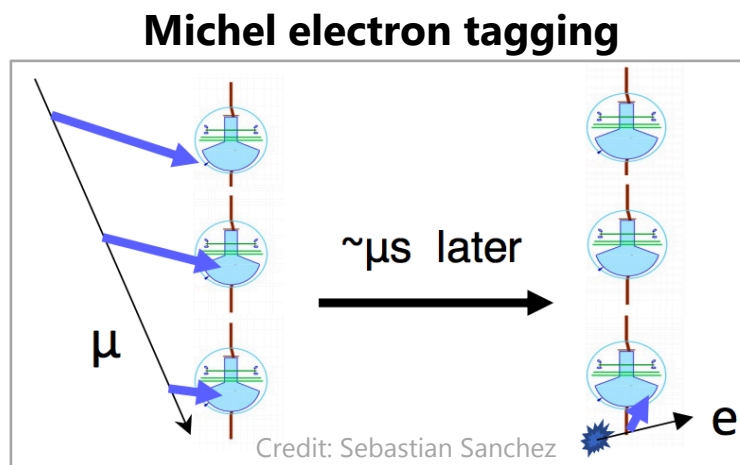
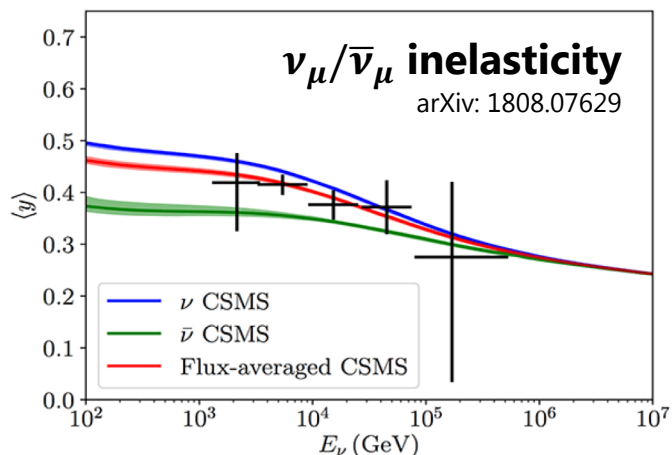
Atmospheric neutrino CPT-V

- As for other Planck scale physics signals, CPT-V effects potentially suppressed at low energies, motivating:
 - High energy atmospheric neutrino tests (e.g. IceCube)
 - Tests of energy-dependent CPT-V phenomenology
- Neither done so far**



Atmospheric neutrino CPT-V

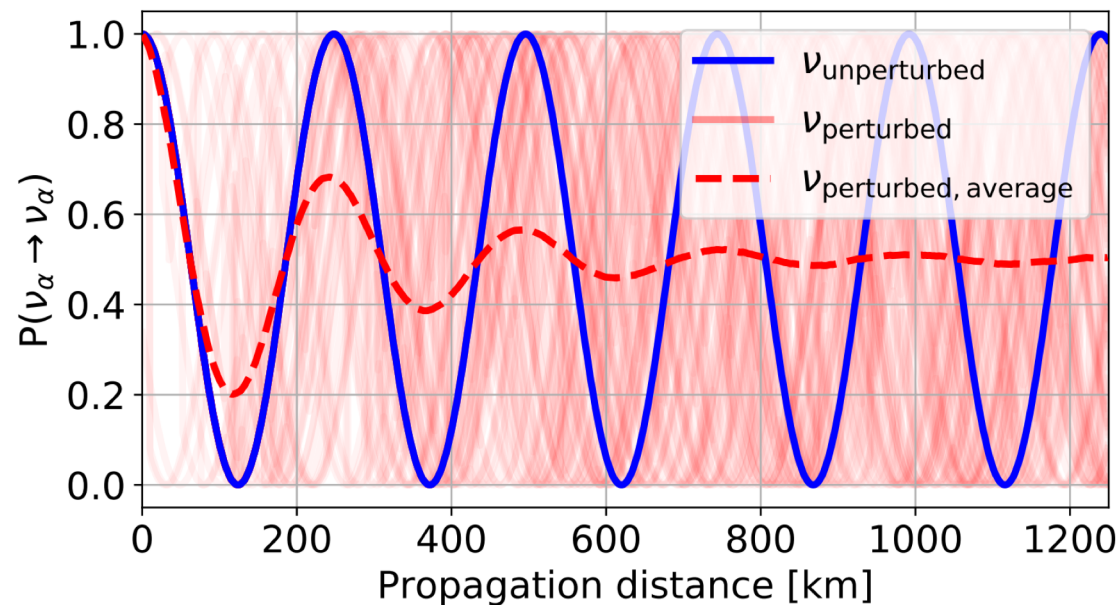
- As for other Planck scale physics signals, CPT-V effects potentially suppressed at low energies, motivating:
 - High energy atmospheric neutrino tests (e.g. IceCube) } **Neither done so far**
 - Tests of energy-dependent CPT-V phenomenology } **Neither done so far**
- Can in principal statistically separate $\nu_\mu/\bar{\nu}_\mu$ samples using indirect information
 - Inelasticity } **IceCube Upgrade!**
 - Michel electron tagging } **IceCube Upgrade!**



Decoherence

Neutrino decoherence

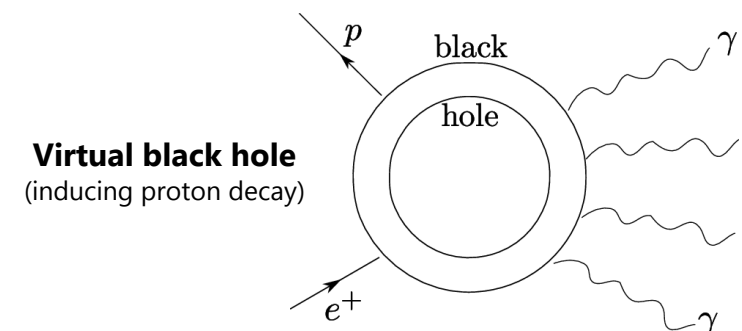
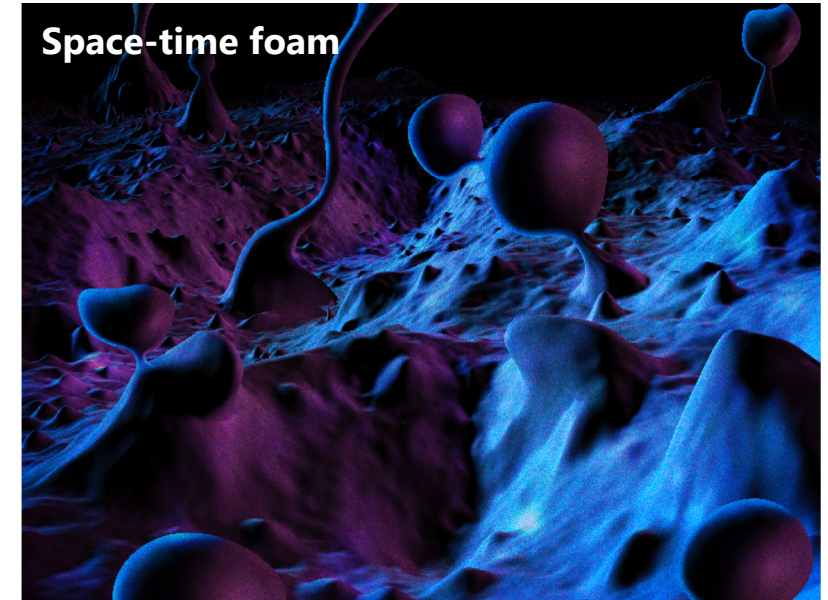
- Neutrino oscillations generally considered to be coherent
 - *The wavefunctions of two neutrinos of the same energy travelling the same path evolve identically*
- Not true for neutrinos propagating in a stochastic medium
 - Neutrino ensemble becomes increasingly out of phase over distance
 - Neutrino decoherence → damping of neutrino oscillations



2-flavor toy model
(not realistic parameters)

What stochastic background?

- Quantum gravity \rightarrow Planck scale space-time fluctuations: **space-time foam**
- Fluctuating space-time curvature \rightarrow fluctuating travel time/distance between two points: **lightcone fluctuations**
 - Velocity fluctuations (stochastic LIV) also considered
- Also potential for **virtual black hole** (VBH) formation
 - QG analogue of vacuum polarisation
 - Space-time permeated with Planck scale black holes
 - Propagating neutrinos undergo stochastic (flavour violating?) interactions with VBH background



Decoherence formalism

- Neutrino decoherence generally treated as **open quantum system**
 - Neutrino and environment considered as single quantum system
- State evolution using **Lindblad master equation**:

$$\dot{\rho} = \underbrace{-i[H, \rho]}_{\text{Standard oscillations}} - \underbrace{\mathcal{D}[\rho]}_{\text{Decoherence operator}}$$

$\rho = \sum_j p_j |\psi_j\rangle \langle \psi_j|$
 State represented using **density matrices**

New physics here!

Decoherence formalism

- Neutrino decoherence generally treated as **open quantum system**
 - Neutrino and environment considered as single quantum system
- State evolution using **Lindblad master equation:**

$$\dot{\rho} = -i[H, \rho] - \mathcal{D}[\rho]$$

$$\mathcal{D}[\rho] = \overbrace{\begin{pmatrix} 0 & \Gamma_{21}\rho_{12} & \Gamma_{31}\rho_{13} \\ \Gamma_{21}\rho_{21} & 0 & \Gamma_{32}\rho_{23} \\ \Gamma_{31}\rho_{31} & \Gamma_{32}\rho_{32} & 0 \end{pmatrix}}$$

Most studies use a general form for the decoherence operator, characterised by damping parameters, Γ

Decoherence formalism

- Neutrino decoherence generally treated as **open quantum system**
 - Neutrino and environment considered as single quantum system
- State evolution using **Lindblad master equation:**

$$\dot{\rho} = -i[H, \rho] - \mathcal{D}[\rho]$$

$$\mathcal{D}[\rho] = (D_{\mu\nu} \rho^\nu) b^\mu$$

$$D = \begin{pmatrix} \Gamma_0 & \beta_{01} & \beta_{02} & \beta_{03} & \beta_{04} & \beta_{05} & \beta_{06} & \beta_{07} & \beta_{08} \\ \beta_{01} & \Gamma_1 & \beta_{12} & \beta_{13} & \beta_{14} & \beta_{15} & \beta_{16} & \beta_{17} & \beta_{18} \\ \beta_{02} & \beta_{12} & \Gamma_2 & \beta_{23} & \beta_{24} & \beta_{25} & \beta_{26} & \beta_{27} & \beta_{28} \\ \beta_{03} & \beta_{13} & \beta_{23} & \Gamma_3 & \beta_{34} & \beta_{35} & \beta_{36} & \beta_{37} & \beta_{38} \\ \beta_{04} & \beta_{14} & \beta_{24} & \beta_{34} & \Gamma_4 & \beta_{45} & \beta_{46} & \beta_{47} & \beta_{48} \\ \beta_{05} & \beta_{15} & \beta_{25} & \beta_{35} & \beta_{45} & \Gamma_5 & \beta_{56} & \beta_{57} & \beta_{58} \\ \beta_{06} & \beta_{16} & \beta_{26} & \beta_{36} & \beta_{46} & \beta_{56} & \Gamma_6 & \beta_{67} & \beta_{68} \\ \beta_{07} & \beta_{17} & \beta_{27} & \beta_{37} & \beta_{47} & \beta_{57} & \beta_{67} & \Gamma_7 & \beta_{78} \\ \beta_{08} & \beta_{18} & \beta_{28} & \beta_{38} & \beta_{48} & \beta_{58} & \beta_{68} & \beta_{78} & \Gamma_8 \end{pmatrix}$$

**Decomposition in SU(N)
basis also often used**

Decoherence formalism

- Neutrino decoherence generally treated as **open quantum system**
 - Neutrino and environment considered as single quantum system

- State evolution using **Lindblad master equation**:

$$\dot{\rho} = -i[H, \rho] - \mathcal{D}[\rho]$$

- Energy-dependence typically added “by hand”:

$$\Gamma(E) = \Gamma(E_0) \left(\frac{E}{E_0} \right)^n \quad \text{or} \quad \Gamma(E) = \zeta_{\text{Planck}} \frac{E^n}{M_{\text{Planck}}^{n-1}}$$

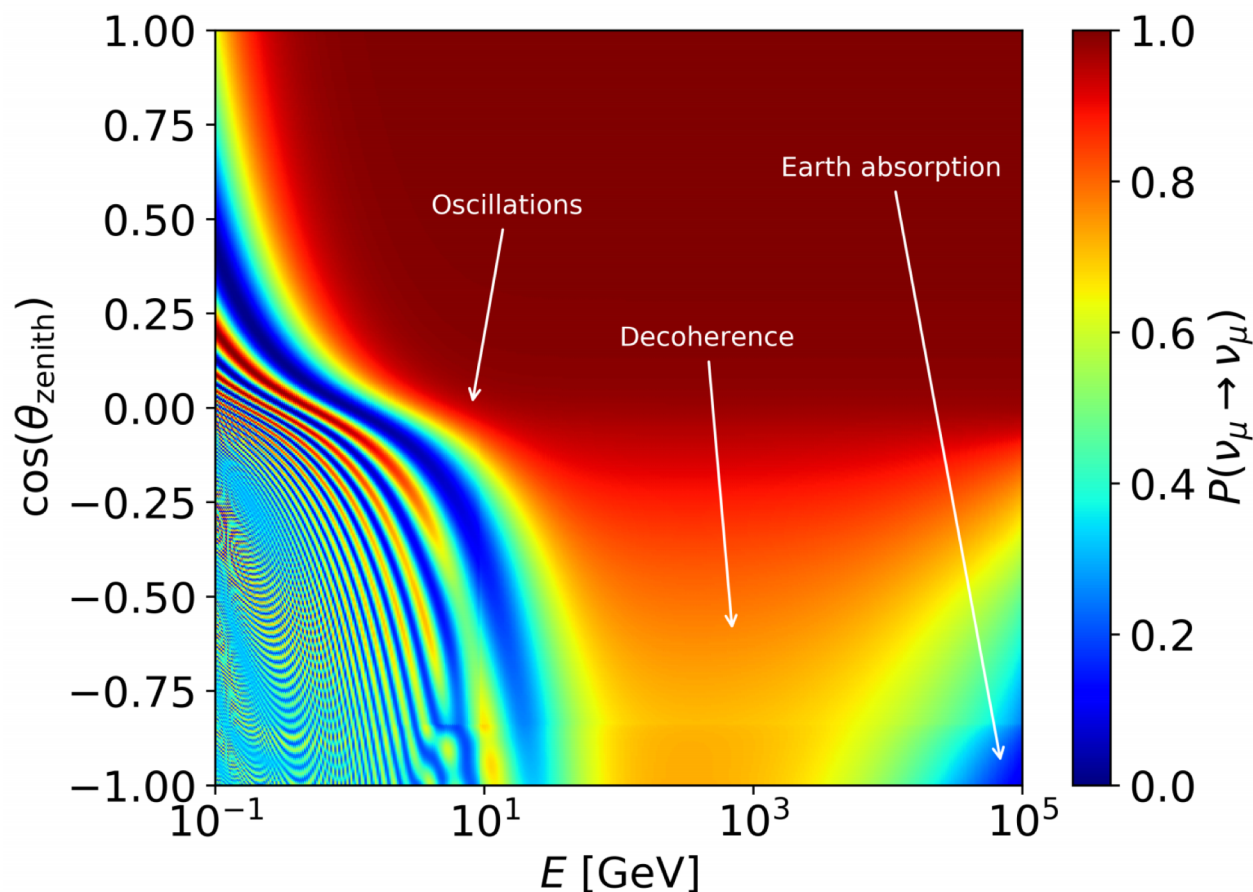
w.r.t. arbitrary E (usually 1 GeV)

w.r.t. Planck scale

“Natural” expectation: $\zeta \sim \mathcal{O}(1)$

Atmospheric neutrino signal

- Signal is damping of neutrino flavour transitions \rightarrow increases with baseline



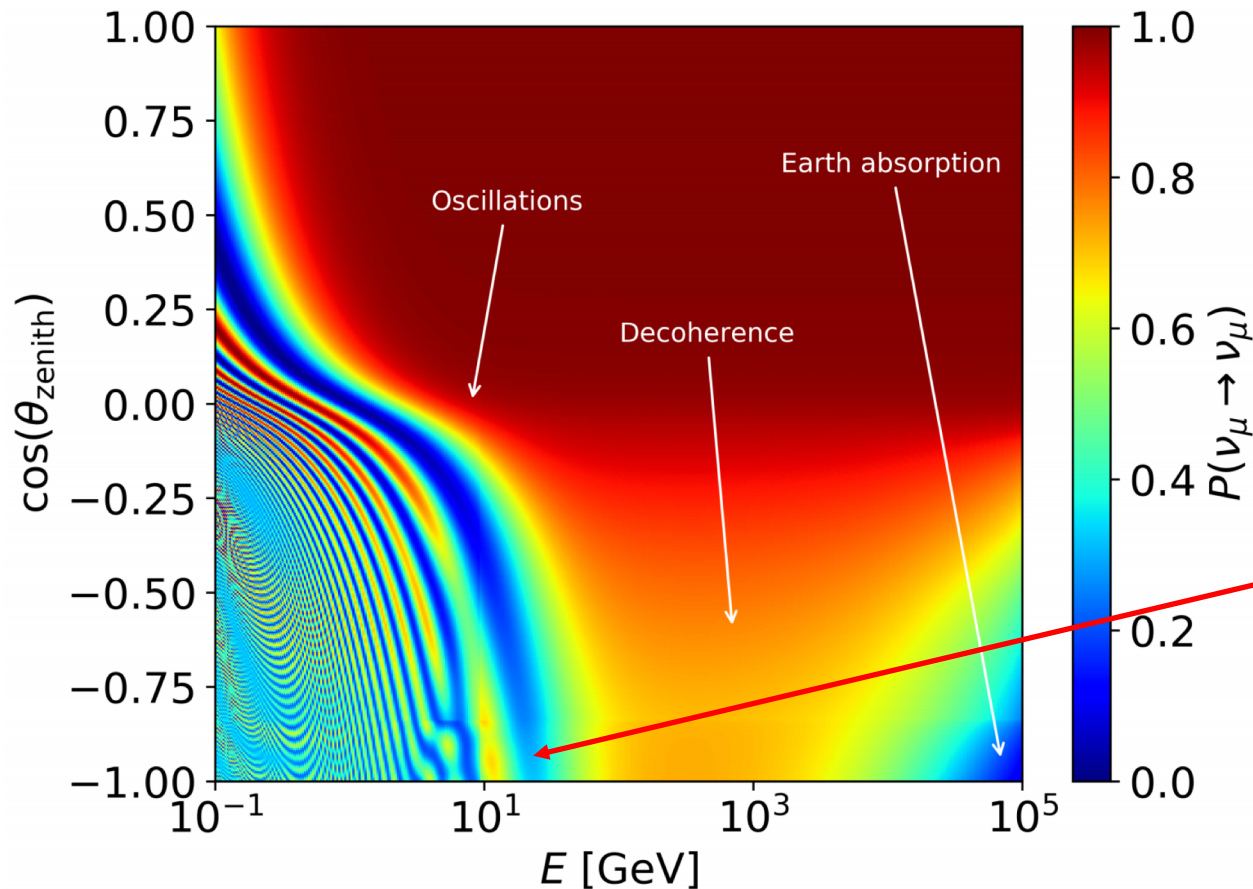
Example scenario 1:

Flavour violating ν -VBH interactions
Energy-independent

Signal across all E
(IceCube + DUNE synergy)

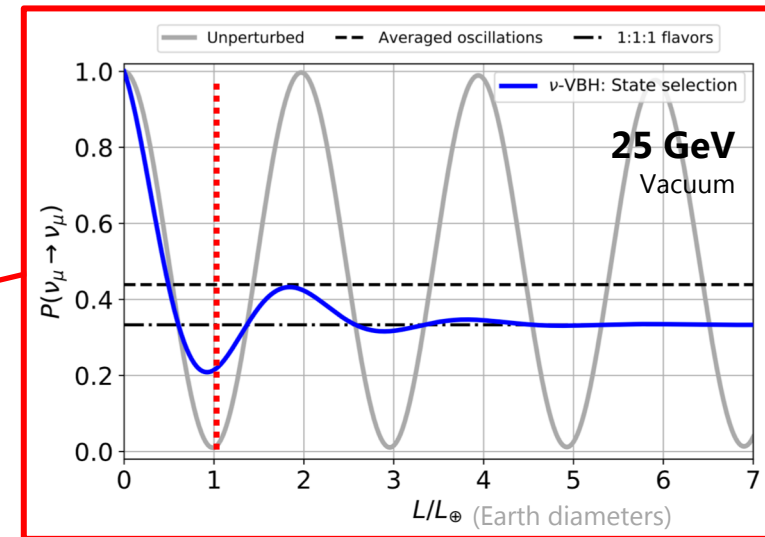
Atmospheric neutrino signal

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Example scenario 1:

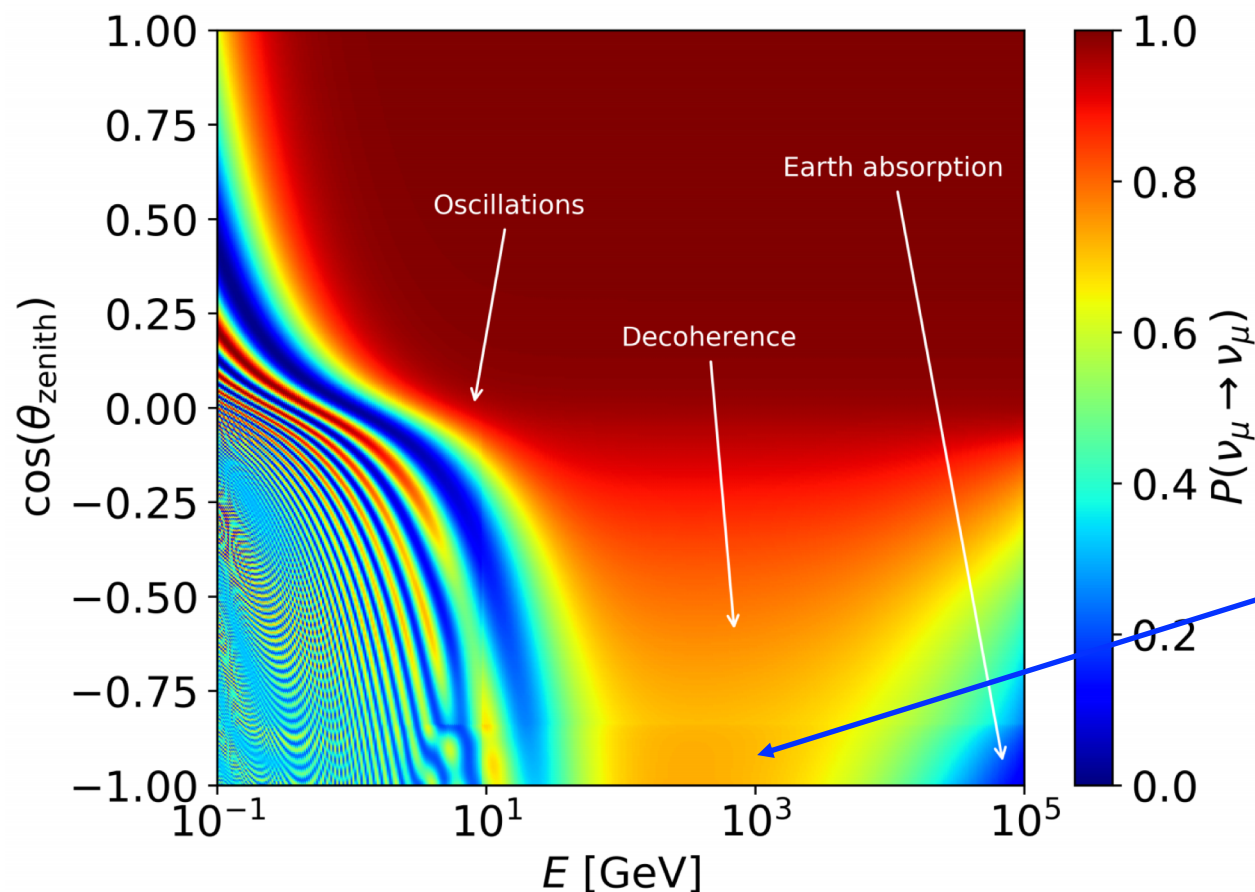
Flavour violating ν -VBH interactions
Energy-independent



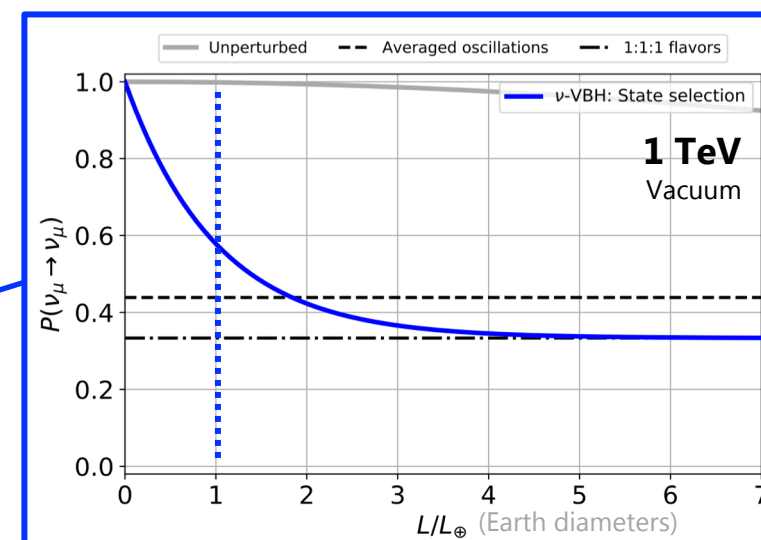
Standard oscillations for Earth crossing neutrinos weakened

Atmospheric neutrino signal

- Signal is damping of neutrino flavour transitions \rightarrow increases with baseline



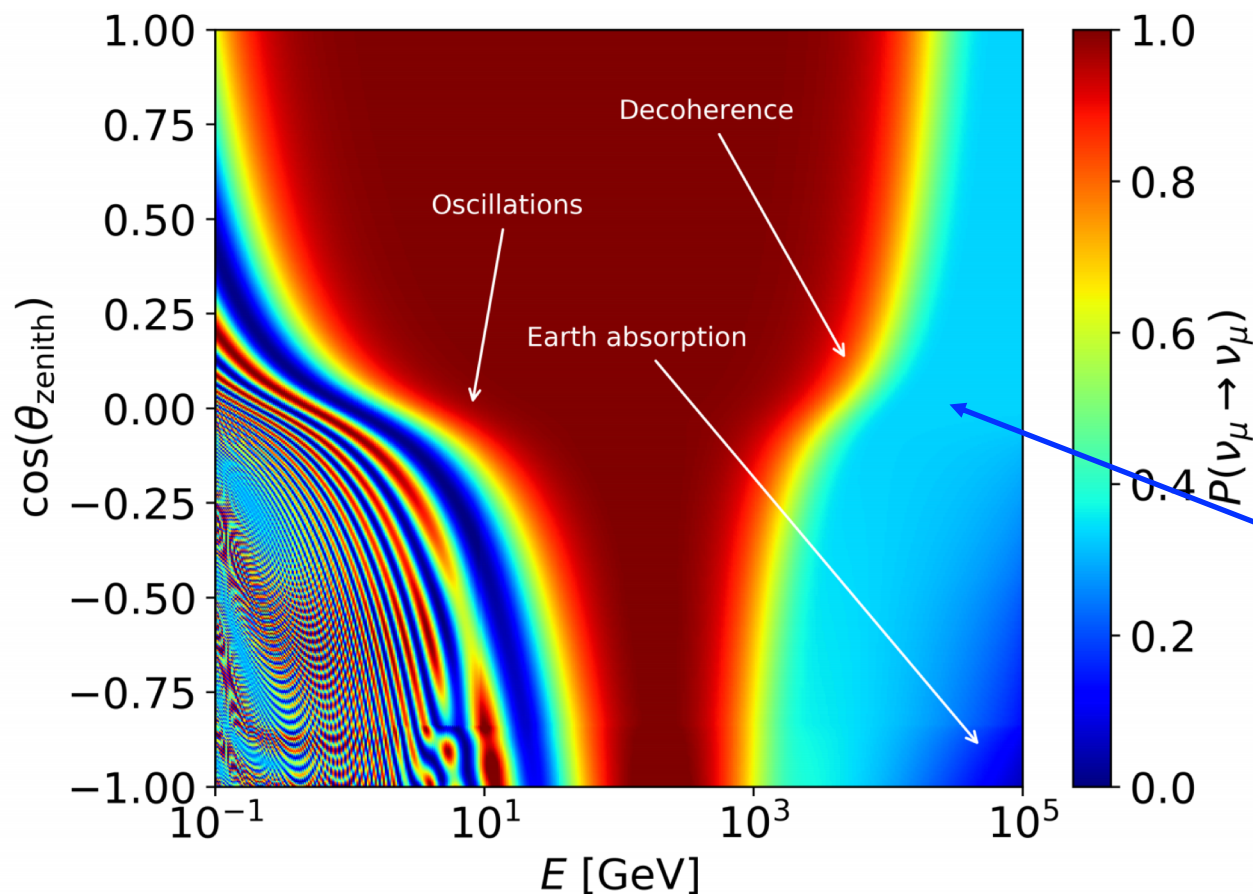
Example scenario 1:
Flavour violating ν -VBH interactions
Energy-independent



Flavour transitions outside of standard oscillation region

Atmospheric neutrino signal

- Signal is damping of neutrino flavour transitions \rightarrow increases with baseline



Example scenario 2:

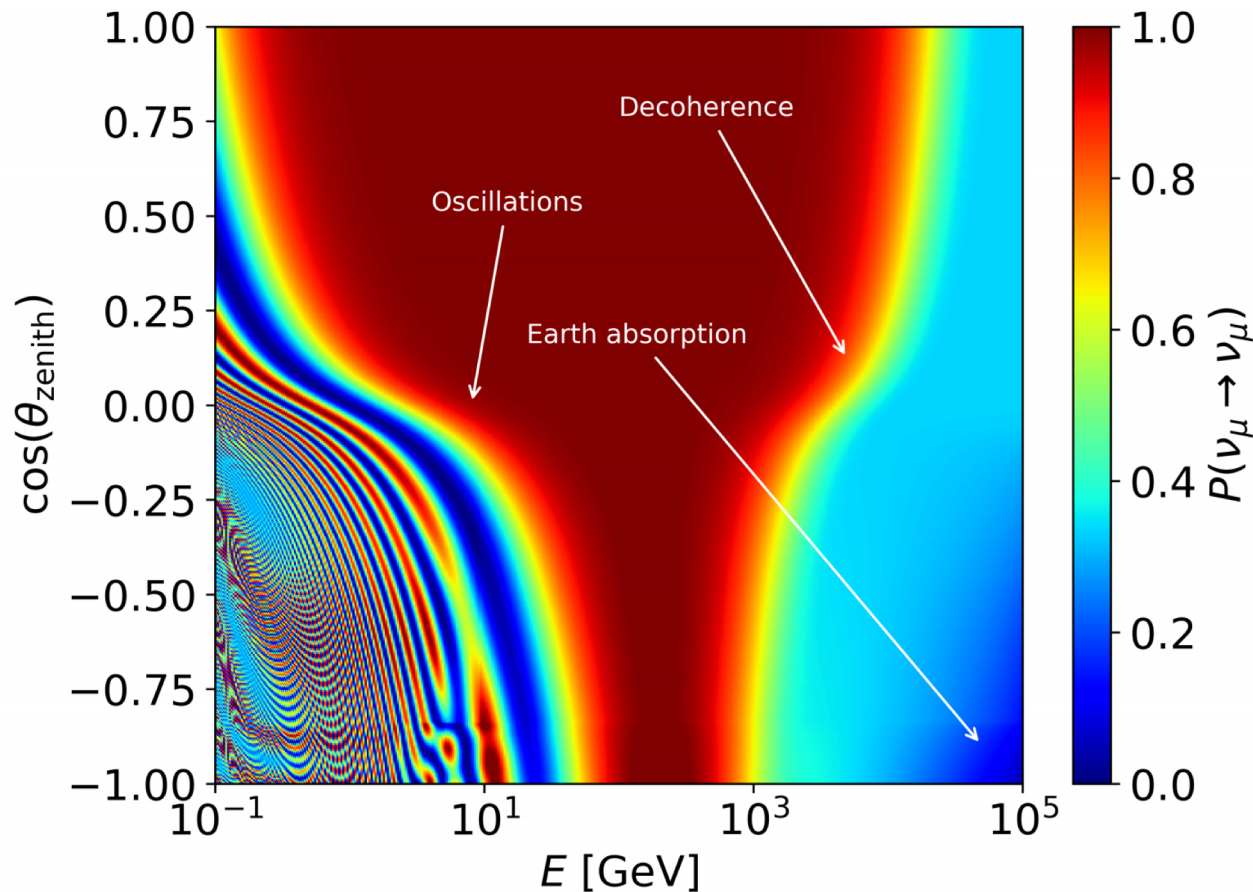
Flavour violating ν -VBH interactions
 E^2 energy-dependence

High-energy flavour transitions outside of standard oscillation region, even for smaller baselines

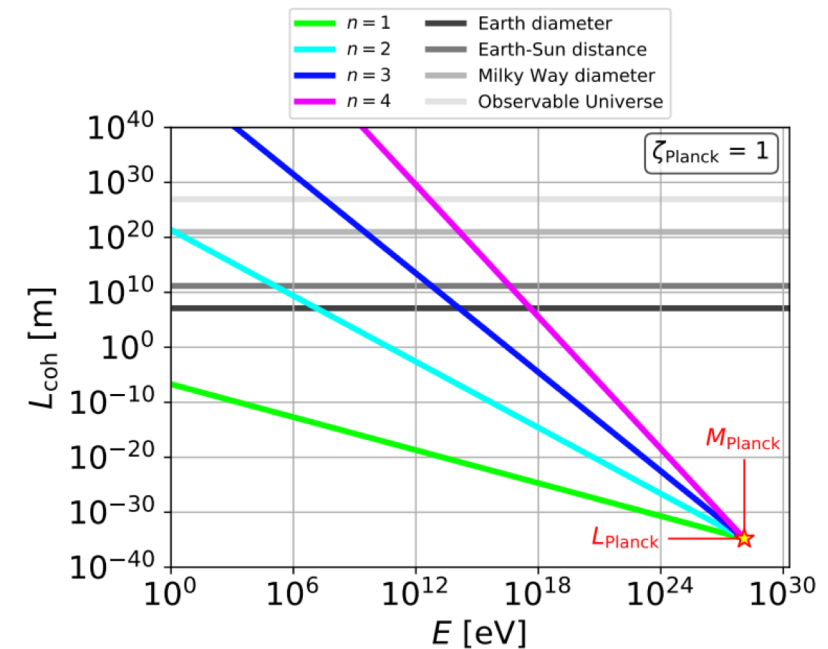
Saturates at $\nu_e : \nu_\mu : \nu_\tau = 1 : 1 : 1$

Atmospheric neutrino signal

- Signal is damping of neutrino flavour transitions \rightarrow increases with baseline



Example scenario 2:
Flavour violating ν -VBH interactions
 E^2 energy-dependence

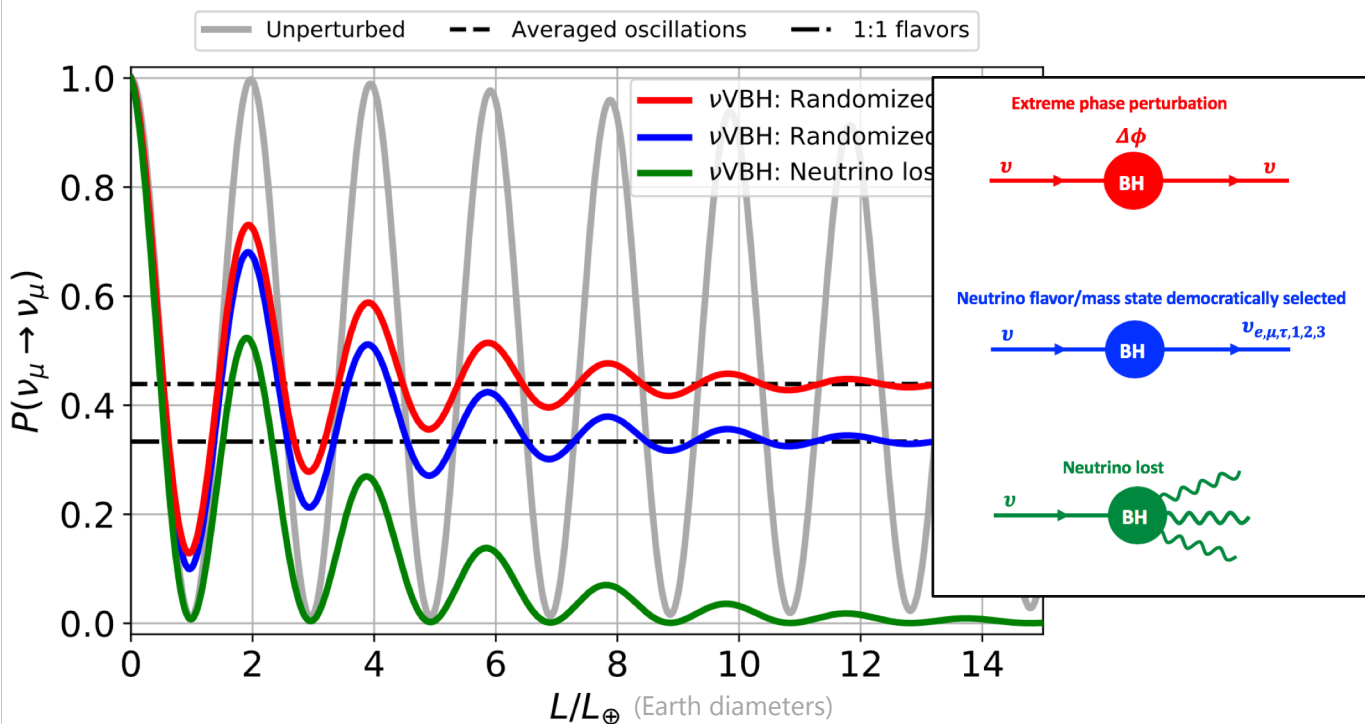


Sensitivity to "natural" Planck scale effects for $E^{\approx 3}$ -dependence!

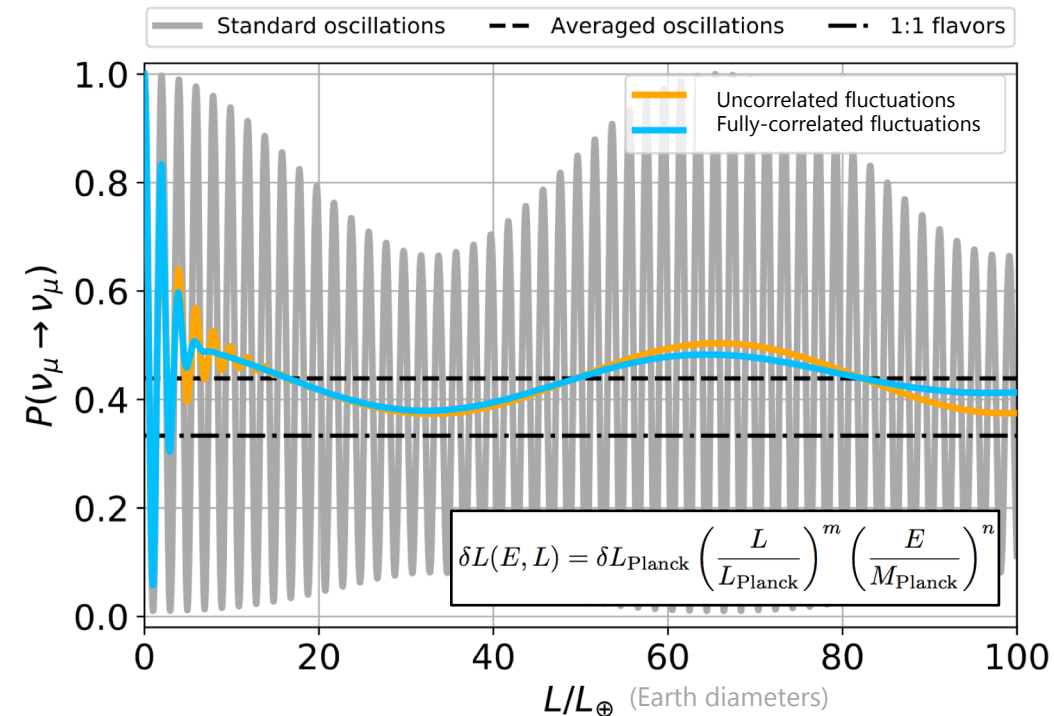
Other scenarios

- Rich decoherence phenomenology depending on underlying microphysics
 - Final flavour, large baseline limit, atmospheric vs solar frequency relative damping, unitarity and energy- and distance-dependence depend on operator/scenario tested

ν – virtual black hole interactions

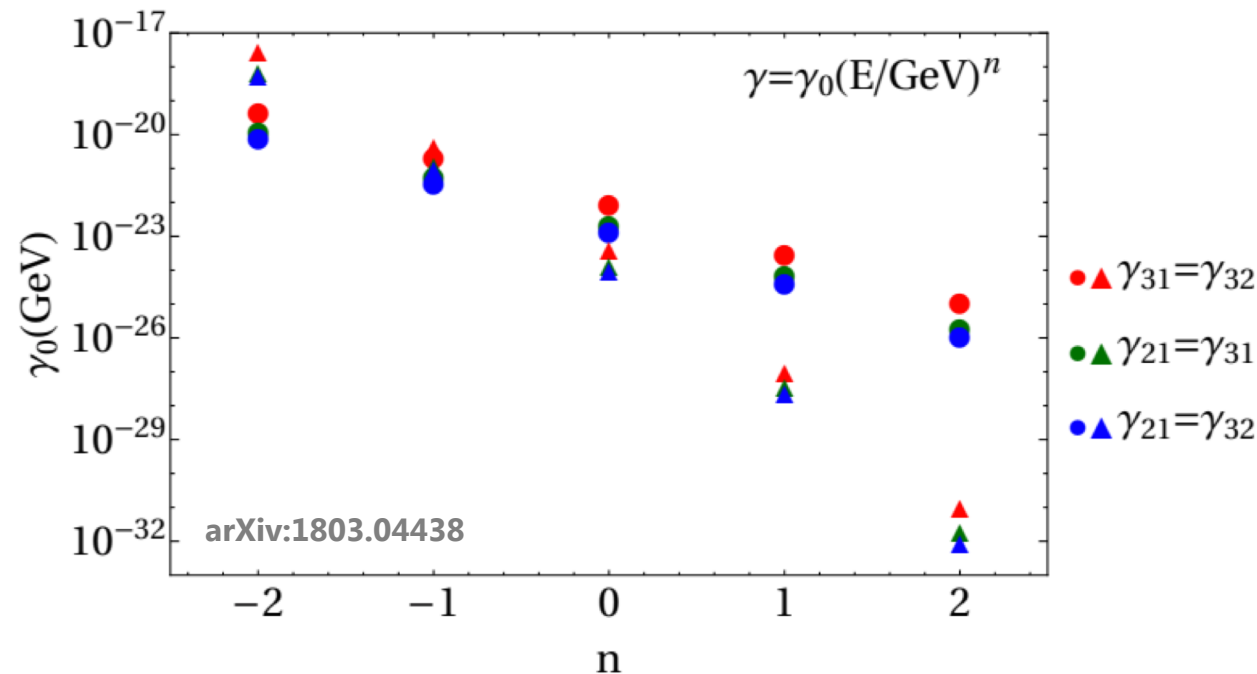


Lightcone fluctuations



Status of atmospheric neutrino searches

- Searches performed with both SuperK and IceCube
 - Most sensitive using 1 yr IceCube + 3 yr DeepCore public datasets
 - Coloma, Lopez-Pavon, Martinez-Soler, Nunokawa



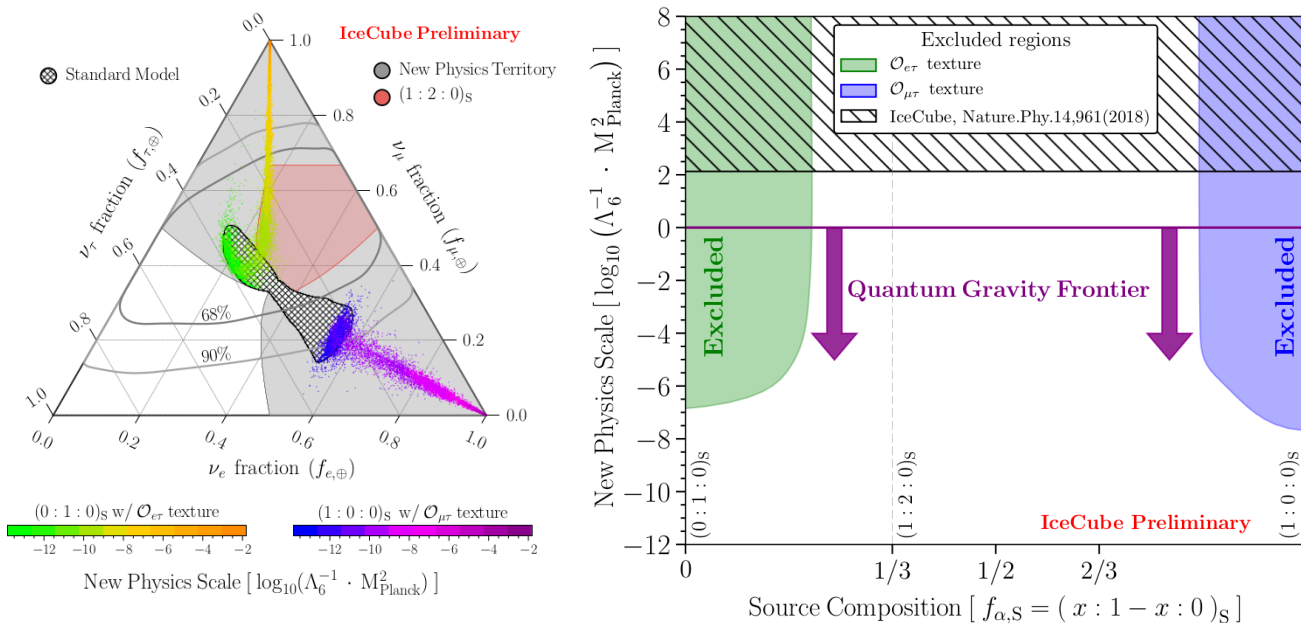
- 8+ yr IceCube collaboration searches underway
 - Testing both specific models and general operators

Wrapping up

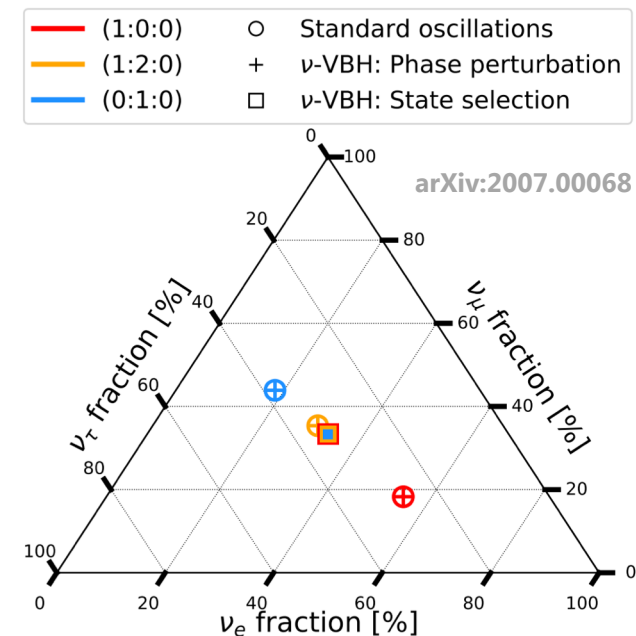
Why not astrophysical neutrinos?

- The extremely high energies and baselines of the diffuse astrophysical neutrino flux is also a great testing ground for new physics
- However, poorly understood flux, incoherent nature of sources and low statistics make atmospheric neutrinos preferable in many cases

LIV



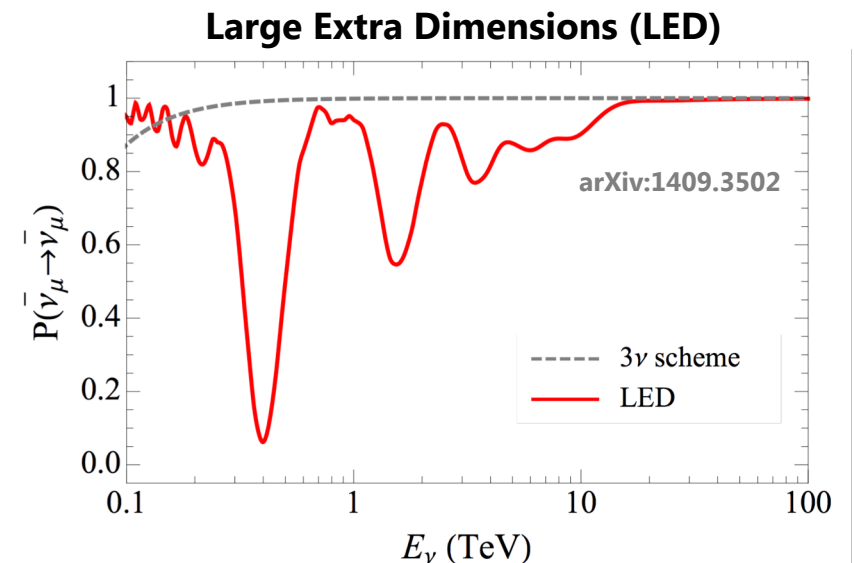
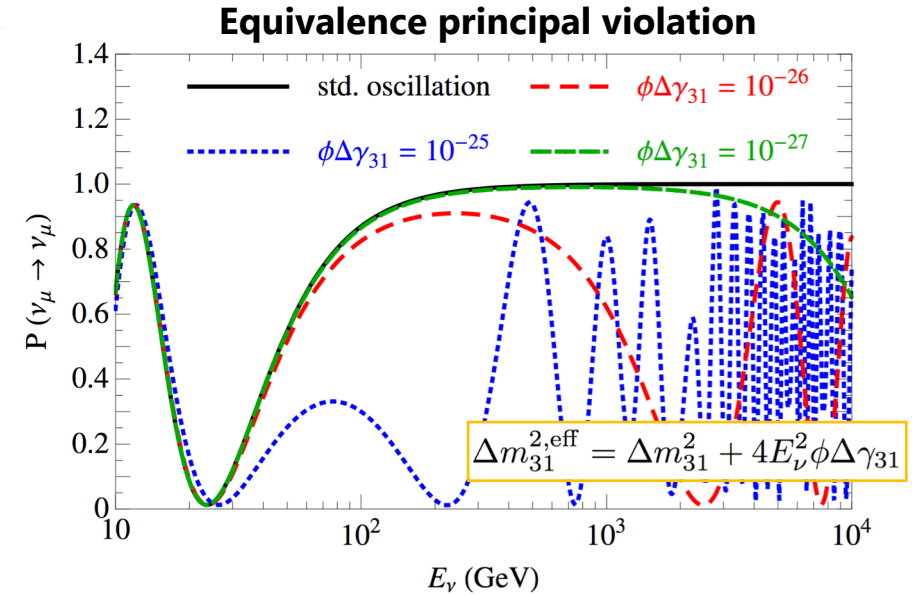
Decoherence



Other related topics

- Equivalence principal violation
 - Inertial mass \neq gravitational mass
- Extra dimensions
 - RH neutrinos access in compactified dimensions
- Proton decay
 - Baryon number violation
- Quantum mechanical tests
 - Leggett-Garg Inequality, ...
-

arXiv:1404.3608

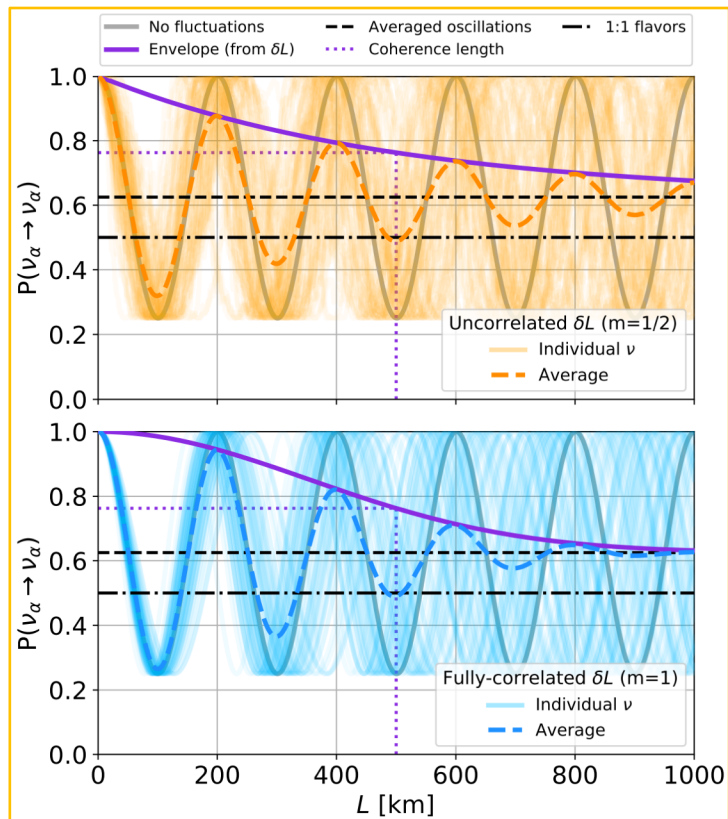


Summary

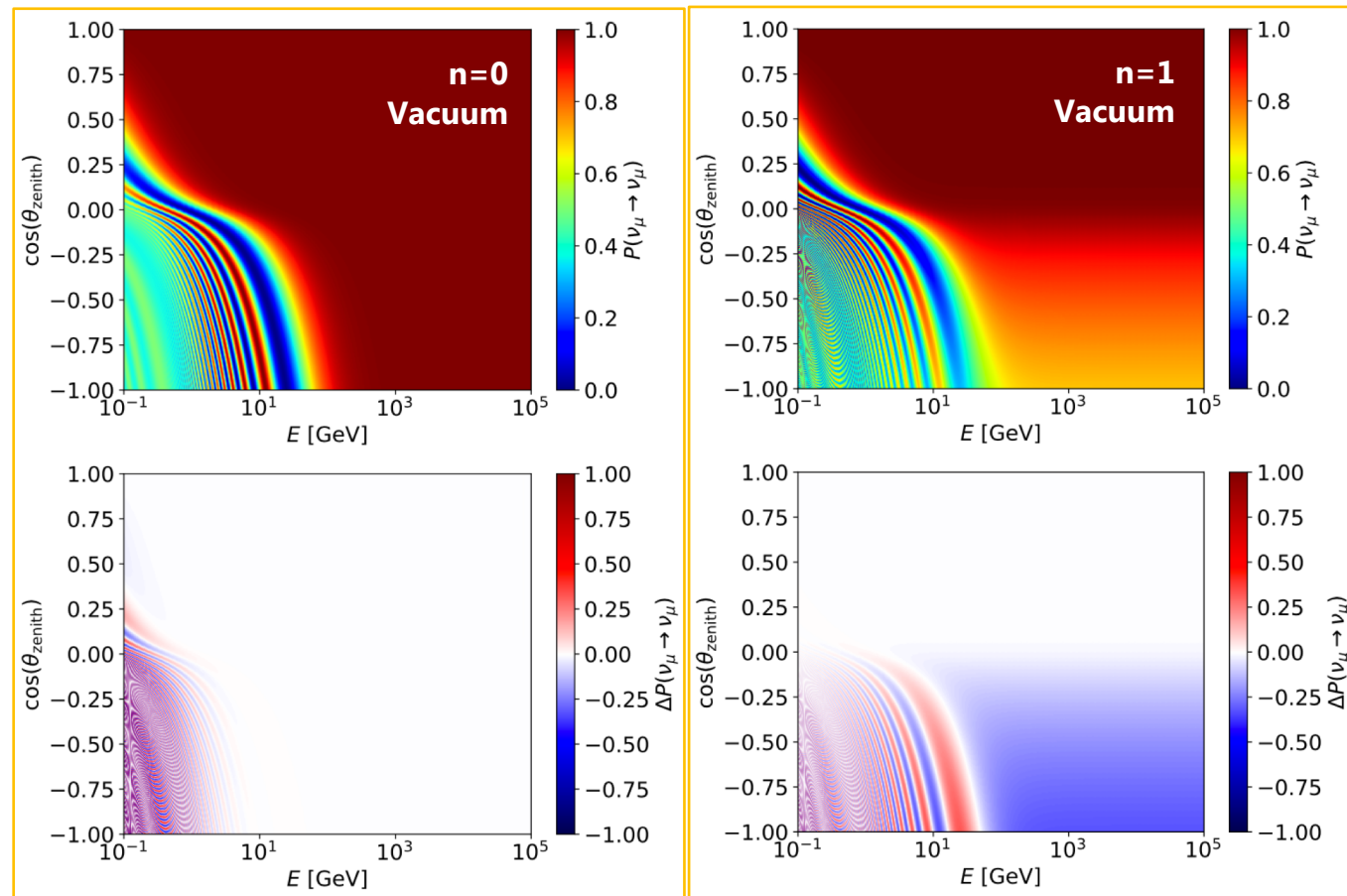
- Many fundamental properties of SM and GR potentially violated in high energy theories such as quantum gravity
 - Suppression at low energies
- Potentially produce sub-dominant modifications to neutrino oscillations
- The high energy, large baseline, high statistics oscillation measurements enabled by atmospheric neutrinos are ideally suited to these searches
 - Some of the strongest tests of Planck scale physics
- Underdeveloped field → plenty of scope for new measurements
- Broad signal energy range → DUNE+IceCube synergy

Back up

Lightcone fluctuations



$$\delta L(E, L) = \delta L_{\text{Planck}} \left(\frac{L}{L_{\text{Planck}}} \right)^m \left(\frac{E}{M_{\text{Planck}}} \right)^n$$



$$\mathcal{D}[\rho] = \frac{2m(\delta L_0)^2 L^{2m-1}}{L_0^{2m}} \left(\frac{E}{E_0} \right)^{2n} \begin{pmatrix} 0 & \frac{\rho_{21}}{(\eta\lambda_{21})^2} & \frac{\rho_{31}}{(\eta\lambda_{31})^2} \\ \frac{\rho_{21}}{(\eta\lambda_{21})^2} & 0 & \frac{\rho_{32}}{(\eta\lambda_{32})^2} \\ \frac{\rho_{31}}{(\eta\lambda_{31})^2} & \frac{\rho_{32}}{(\eta\lambda_{32})^2} & 0 \end{pmatrix}$$