

# Fabry–Pérot Resonators in the Millimeter

---

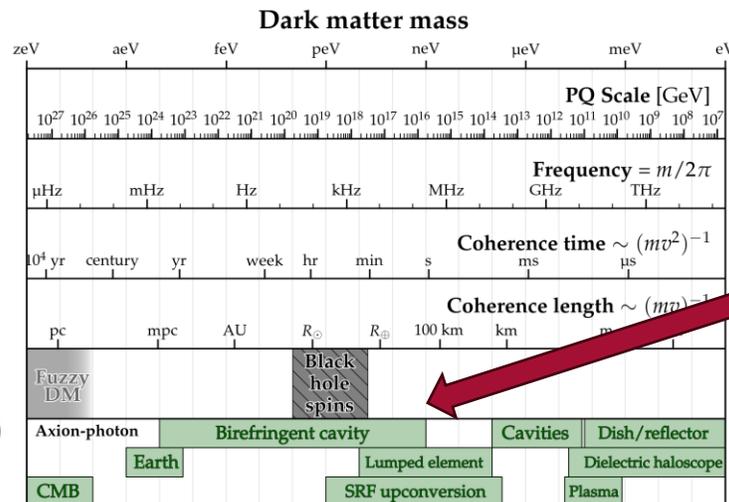
Brodi Elwood

BREAD Collaboration Workshop

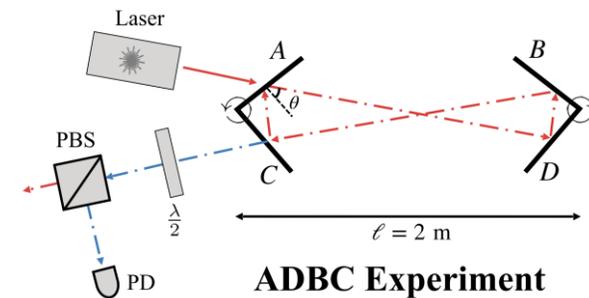
January 14, 2026

# About

- Graduate student at Harvard working in John Kovac's group on the BICEP/Keck series of CMB polarimeters.
- Excited to be here, axion dark matter searches are where I cut my teeth on research.



O'Hare, Zenodo (2020)



Liu, Elwood, Evans & Thaler, *Phys Rev D.* (2019)

# Outline

- Context and motivation for using high-Q resonant cavities for measuring the complex permittivity of dielectrics
- Design and implementation of high-Q Fabry–Pérot resonators
- Measurement technique and results
- Cryogenic measurements
- What's on the horizon?

# Context & motivation

- In the CMB instrumentation community, we are interested in the **index and loss** of dielectrics from room to cryogenic temperatures.
- As receiver sensitivities improve, we become increasingly concerned with the uncertainty on loss in accounting for the white noise in our instruments.
- There is a growing need for rapid, **precise dielectric characterization under realistic operating conditions** to enable informed material selection for receiver optical design.
- Related applications of precise complex permittivity measurements in general mm/sub-mm instrumentation, such as with VLBI, line-intensity mapping, axion searches, and wide-field surveys.

# What other complex permittivity measurements are reported in the literature?

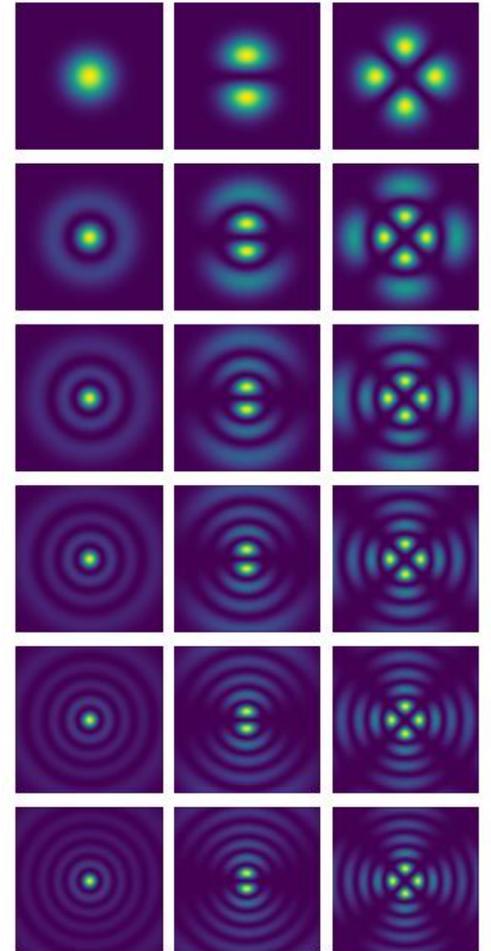
- For example, Lamb (1996) reports for Nylon:

Material	f (GHz)	T (K)	n	$\delta$	$\tan \delta \times 10^4$	Ref.
Nylon	150	290	1.7267	2.9814	101	[36]
	300		1.7266	2.9812	170	
	450		1.7268	2.9814	250	
Nylon	100	300	1.730	2.993	8.8	[15]
	200		1.729	2.993	12.5	
	300		1.729	2.995	16	

- Index and loss depend on a dielectric's formulation, environmental, and thermal history.
  - How does Nylon's equilibrium moisture content impact loss?
- Waveguide-based methods for measuring complex permittivity tend to be narrowband, are impracticable at high frequencies (>75GHz), and suffer increased systematics at cryogenic temperatures.
- Methods using Fourier transform spectrometers suffer increased systematics for low-loss, thin materials.

# Why open resonators?

- We seek a measurement with simple, directly observable quantities that depend strongly on refractive index and loss.
- The standing-wave modes of an open optical resonator are highly sensitive to both cavity optical length and round-trip loss.
- Field buildup in the cavity effectively integrates over many passes through the inserted dielectric sample.
- In particular, the  $TEM_{00}$  (fundamental) modes are readily measured.
  - By measuring how the resonance modes shift and broaden when the cavity is loaded, we can infer the sample material's index and loss.
- Inherently broadband

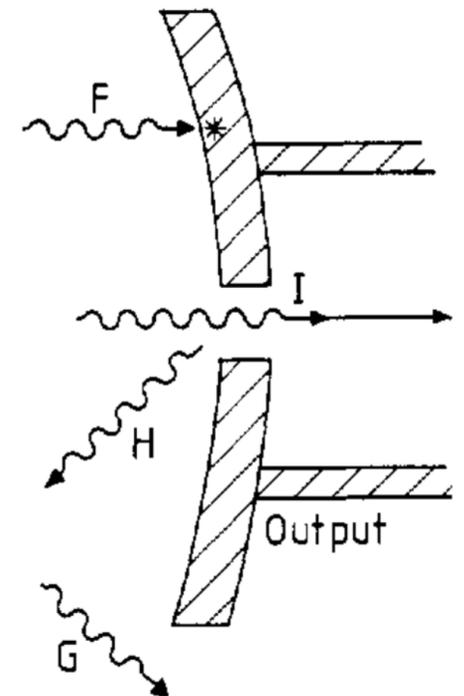
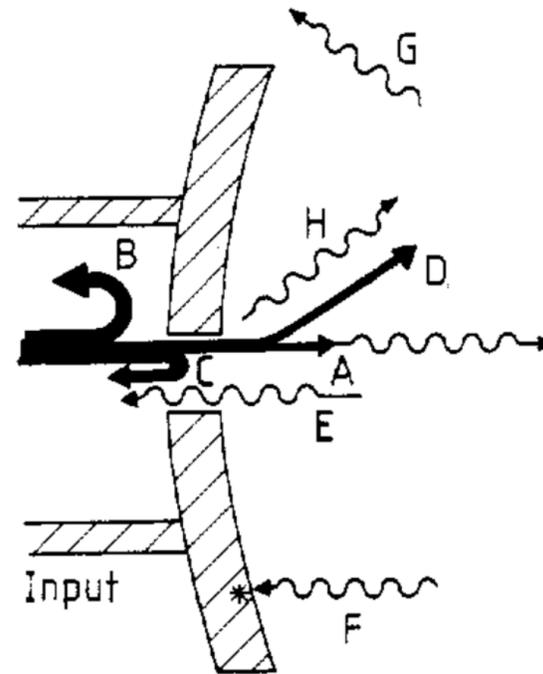


# Outline

- Context and motivation for using high-Q resonant cavities for measuring the complex permittivity of dielectrics
- Design and implementation of high-Q Fabry–Pérot resonators
- Measurement technique and results
- Cryogenic measurements
- What's on the horizon?

# Losses in resonant cavities

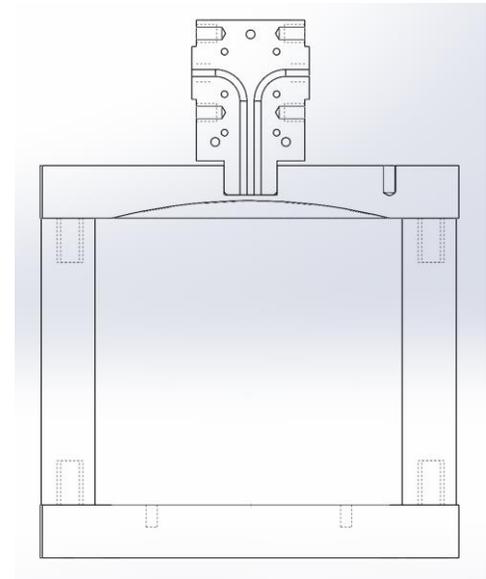
- To measure low-loss dielectrics, we must have high intrinsic quality factor.
  - Minimize cavity power losses and ensure effective coupling.
- We construct cavity quality factor such that we can measure low-loss materials while retaining enough transmitted power to stay above the transmission background of the apparatus.
- Must account for the sources of power loss intrinsic to the cavity:
  - Coupling losses from the aperture
  - Diffractive losses off the edges of the mirror and apertures
  - Resistive or scattering losses on the mirror surfaces



Clarke & Rosenberg (1982)

# Designing a high-Q cavity

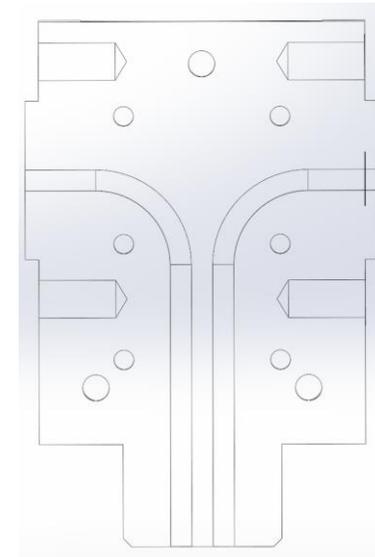
- We can limit diffraction losses by making the mirrors "large":
  - For mm-wave hemispherical cavities of reasonable lengths, the spot size at the spherical mirror is approx. 15 mm.
  - A spherical mirror diameter of approx. 50 mm results in minimal diffraction losses.
- In practice, intrinsic cavity loss is dominated by mirror losses and coupling.
- For our applications, the goal is to measure loss tangents on the order of  $\approx 10^{-5}$ , which requires a cavity with a Q-factor of  $\sim 100,000$ .



# The coupling interface

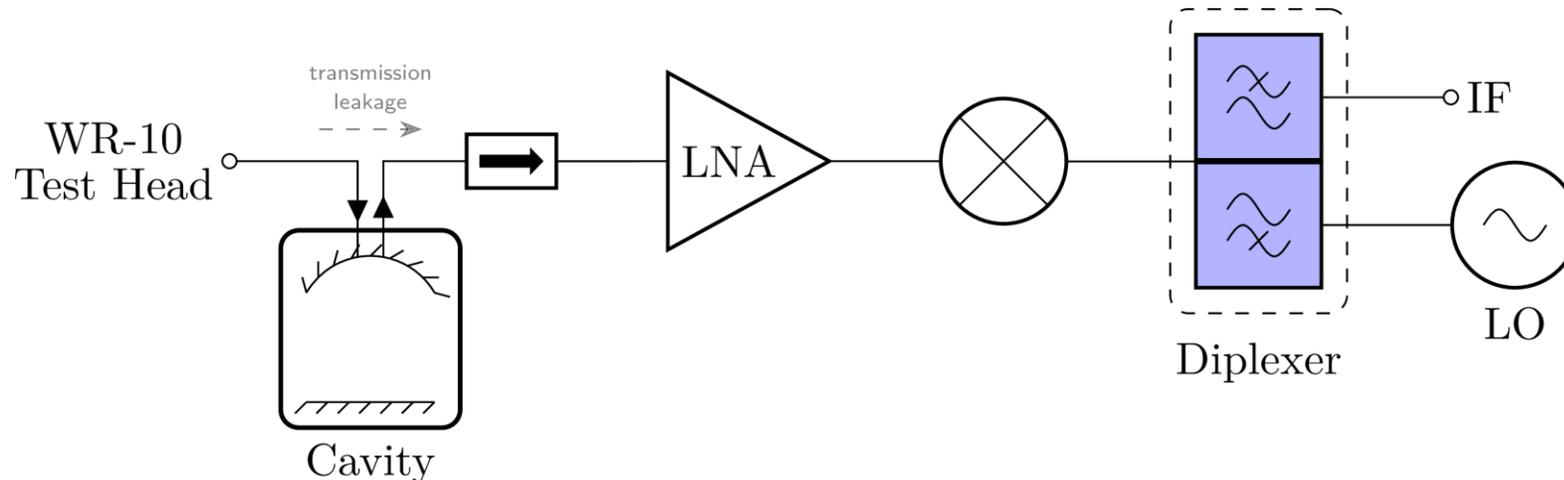
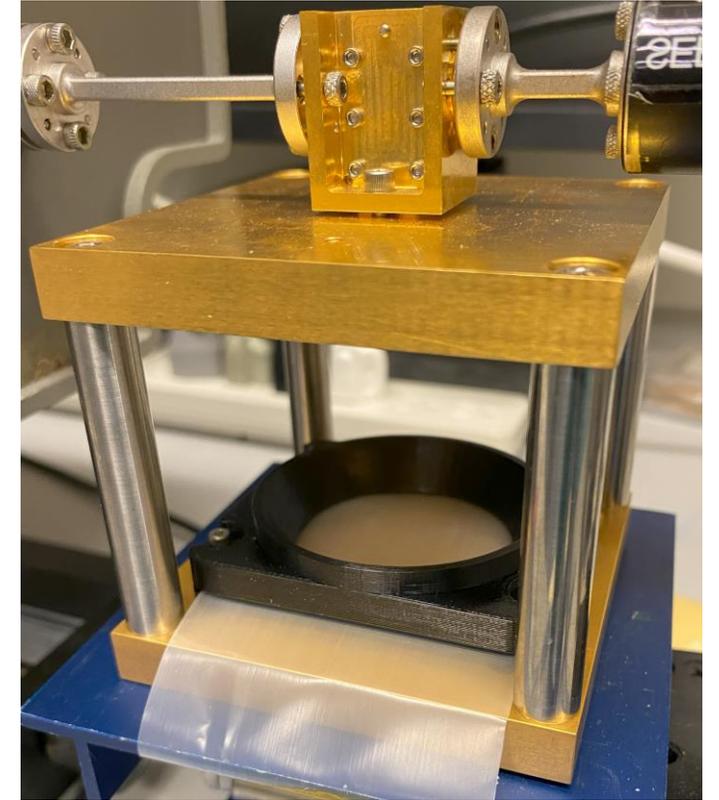
- Radiation is coupled into the cavity via a split-block waveguide butted into a recess in the spherical mirror.
- The coupling constant  $\beta$  (the ratio of cavity incident power to intrinsic power lost) parametrizes the power coupled into the cavity.
  - We use EMS to determine the aperture dimensions that give us the desired coupling.
  - Design balances sufficient signal coupling against the need to minimize cavity loss.

$$Q_L = \frac{1}{1+\beta} Q_0$$



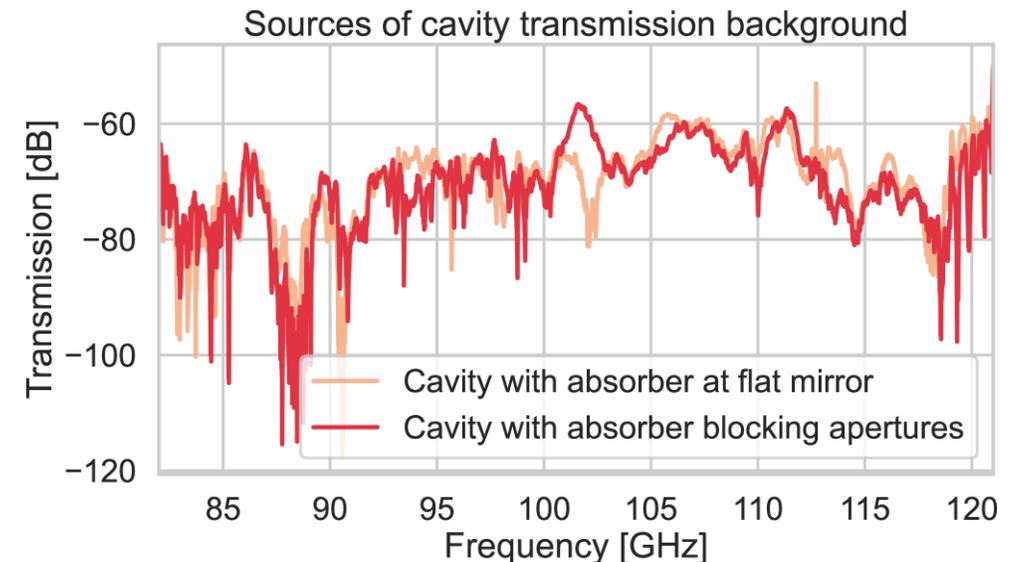
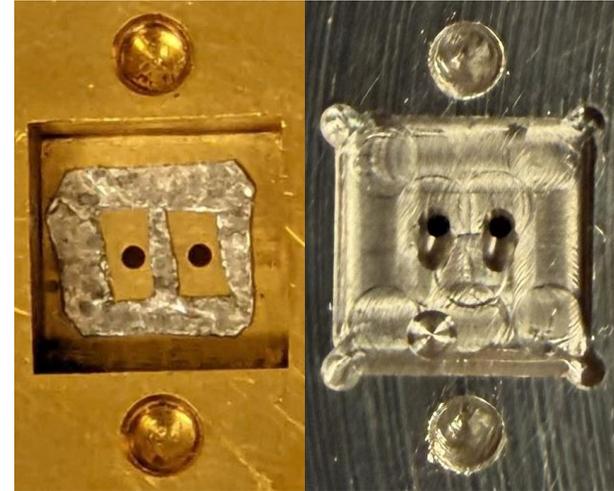
# Quasioptical resonant cavities

- A planar and a spherical mirror, separated by Invar struts, form a hemispherical open resonator.
- A low CTE material was chosen for the struts to minimize temperature-induced fluctuations in cavity length, which directly lead to fluctuations in resonant frequency.
- Dielectric samples are pressed against the flat mirror with a bracket fastened to the edges of the planar surface.



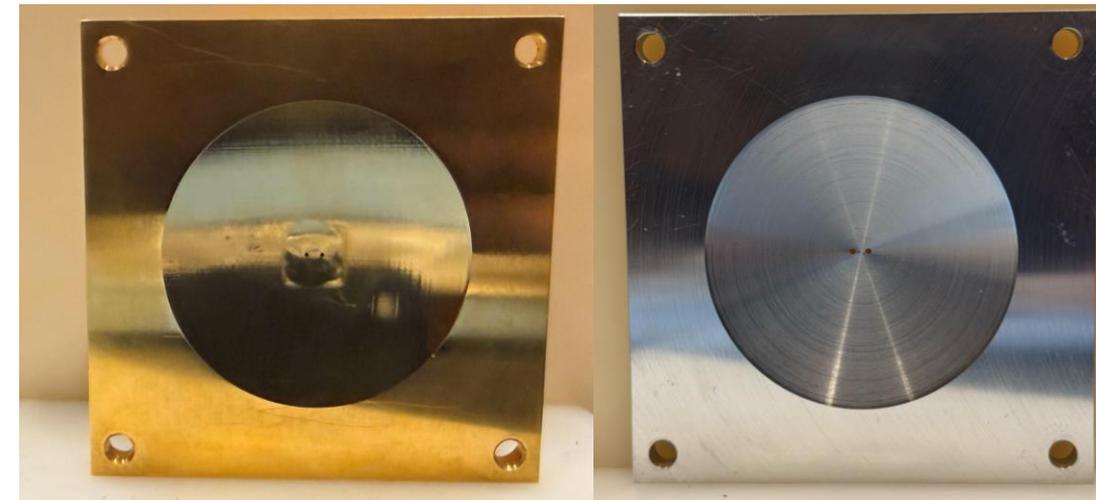
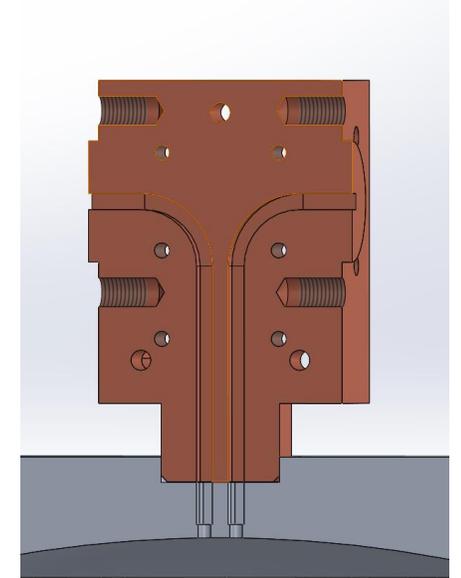
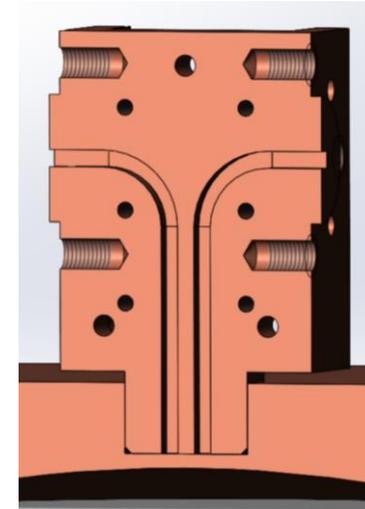
# Mirror & coupling design

- High Q cavities output little power at the receiver; we can easily swamp out the signal by coupling power directly from the transmitter.
- There is coupling between the transmit and receive side at the mirror-coupling block interface.
- Without mitigation for this coupling, we cannot see the resonances!



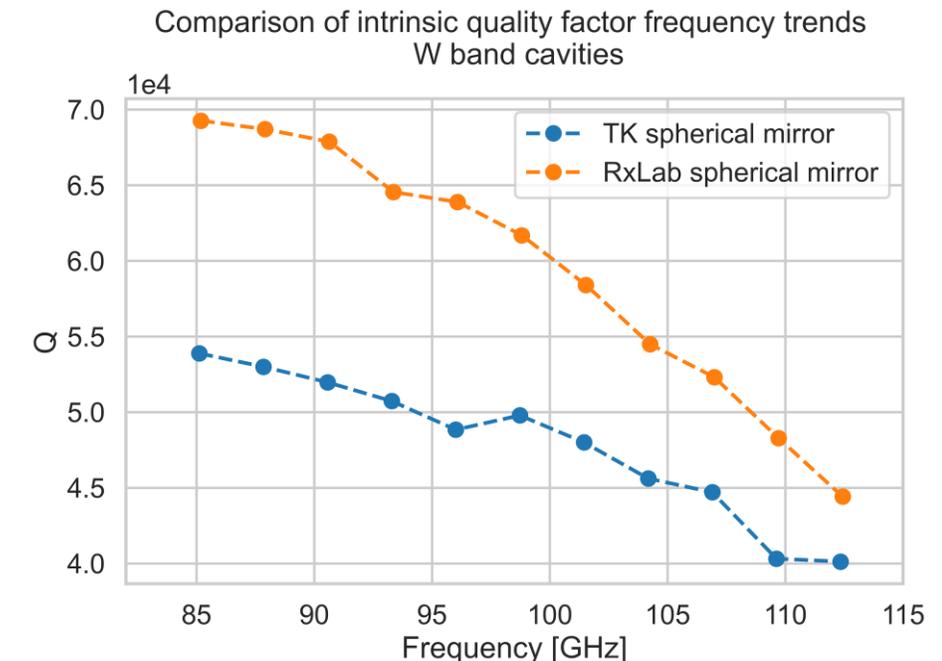
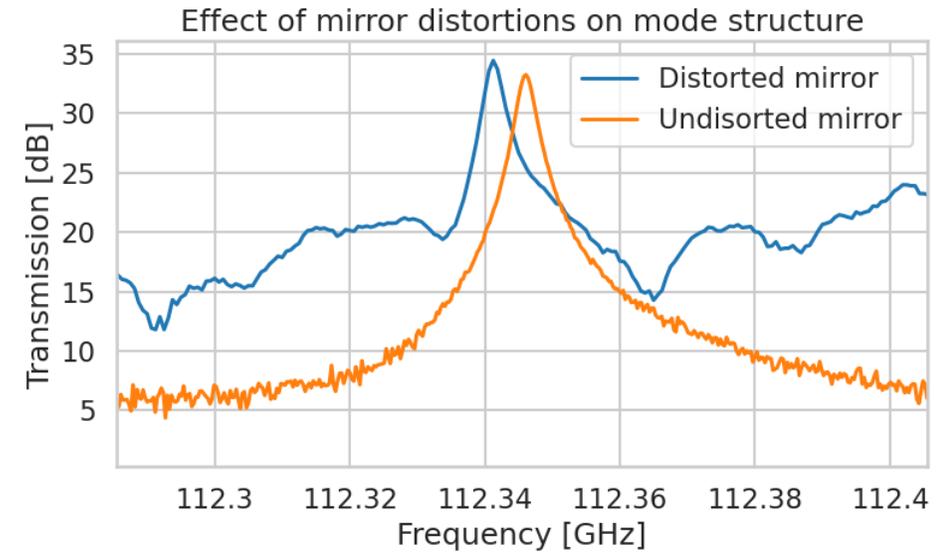
# Improving mirror design

- Suppressing direct transmission requires good contact pressure on the mirror-coupling block interface.
- Increased attenuation by using a small indium gasket.
- Unfortunately, attempting a high-pressure mate tended to distort the spherical mirror.
- Solution: increase depth by machining waveguide structures into the spherical mirror.



# Improved mirror design performance

- Demonstrated that the improved design performs to spec for W band.
- Mirrors are machined in-house, so we can rapidly iterate on designs.
  - Decided to use Al for ease of machining and increased hardness.
- New design more robust to reassembly of cavity or general mechanical perturbations to the coupling block (such as experienced on cooldown).
- Indium gasket no longer necessary, but we still would like ~60 dB of suppression.
  - Working on modeling choke structures in parallel.

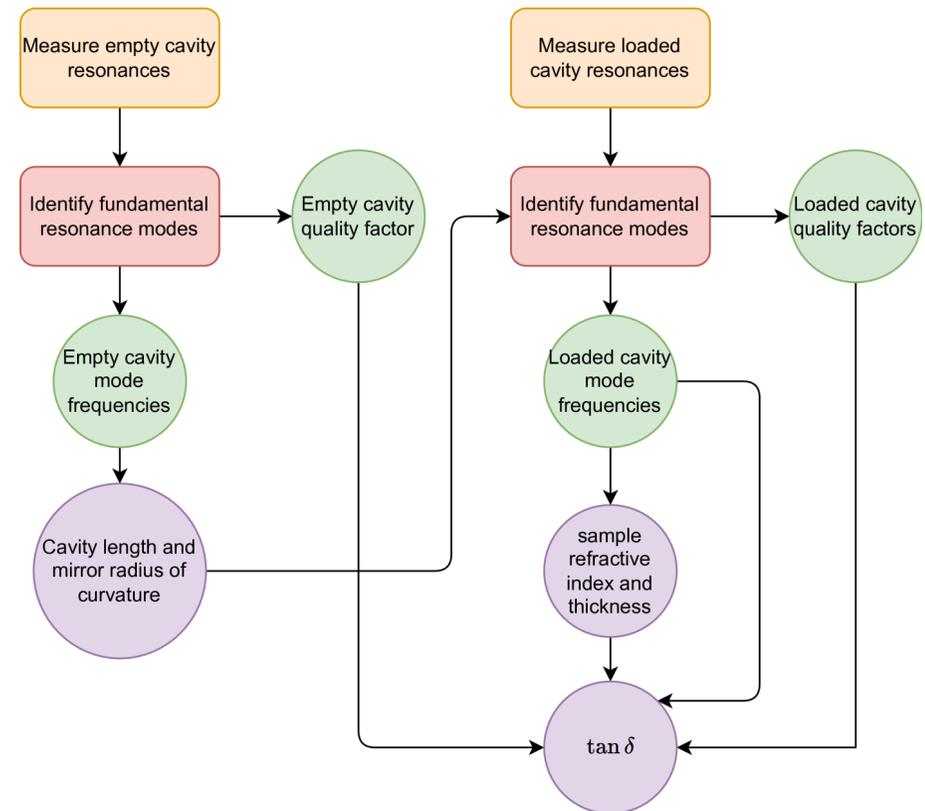


# Outline

- Context and motivation for using high-Q resonant cavities for measuring the complex permittivity of dielectrics
- Design and implementation of high-Q Fabry–Pérot resonators
- **Measurement technique and results**
- Cryogenic measurements
- What's on the horizon?

# Overview of measurement procedure

- By perturbing the cavity with a dielectric sample, we can compare the loaded and unloaded fundamental modes to infer index and loss.
- Practically, two approaches to scanning cavity modes: sweep in frequency or sweep in cavity length.
  - **Frequency-variation method**
    - Natural way to approach with a VNA
  - Length variation method
    - Harder to implement, but cavity intrinsic coupling is the same between loaded and unloaded configurations, reducing systematics when measuring loss.



# Index & loss results

## W-band Measurements

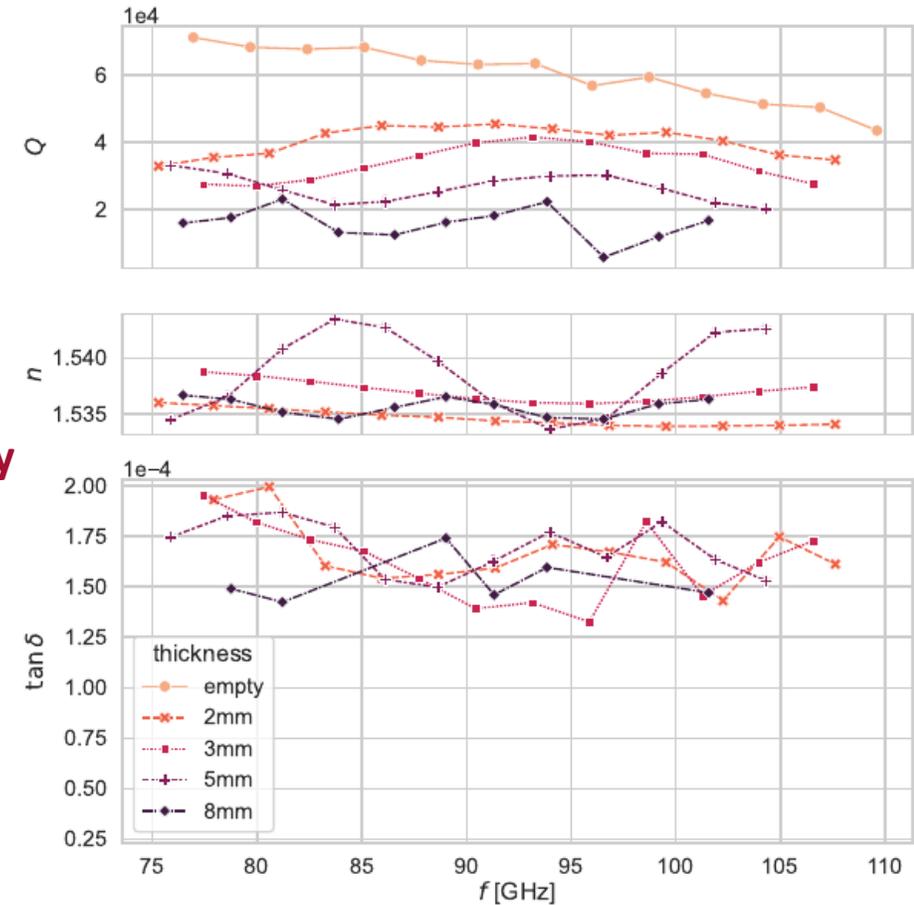
material	$n$	$\tan \delta$ ( $\times 10^{-4}$ )	loss (dB)
HDPE	$1.537 \pm 0.003$	$1.66 \pm 0.18$	-31
annealed HDPE	$1.541 \pm 0.004$	$1.48 \pm 0.24$	-32
UHMWPE	$1.526 \pm 0.007$	$1.43 \pm 0.21$	-32
LDPE			-52
low-loss Si	$3.4230 \pm 0.0001$	$1.47 \pm 0.63$	-30
Kyocera A479G Alumina	$3.140 \pm 0.005$	$3.94 \pm 0.60$	-

Preliminary

## D-band Measurements

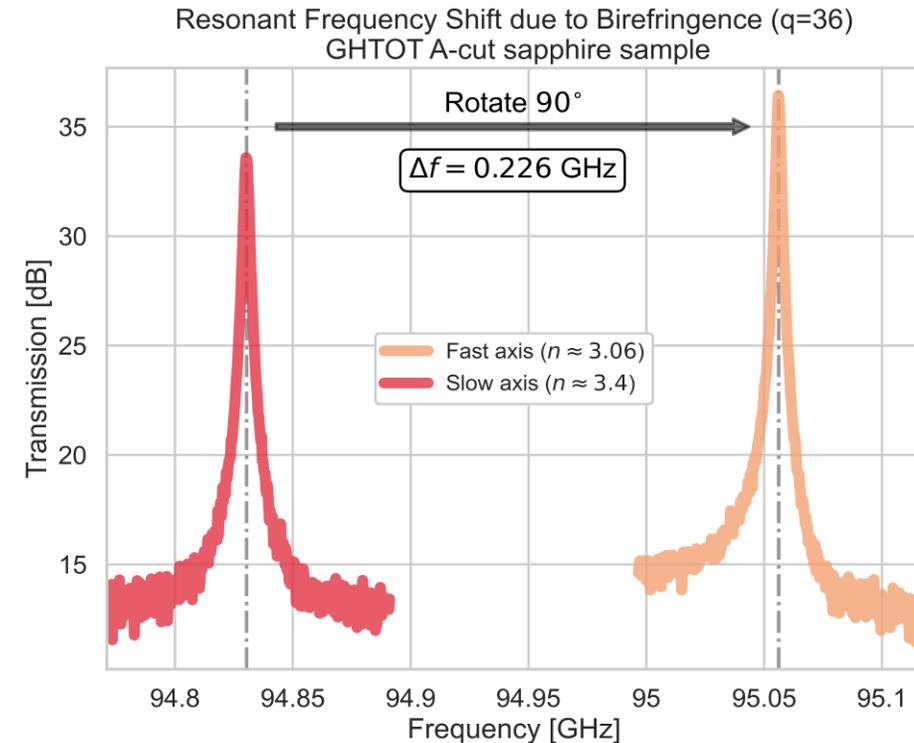
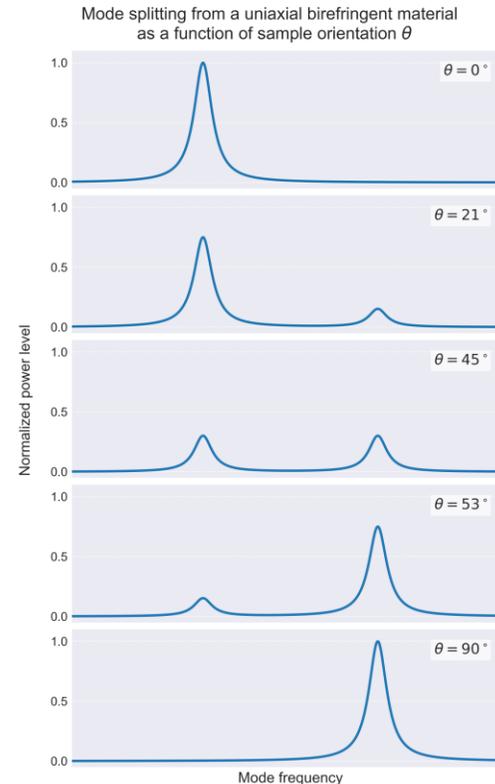
material	$n$	$\tan \delta$ ( $\times 10^{-4}$ )	loss (dB)
GHTOT Sapphire C cut	$3.0647 \pm 0.0007$	$2.3 \pm 1.4$	-

Cavity measurements for 4 samples of HDPE



# Birefringence

- By resolving the electric field vector along a uniaxial sample's two permittivity axes, we can obtain both permittivity values from the resulting two resonance modes.
- We can find the principal axes by rotating until we maximize the power in the fundamental modes.

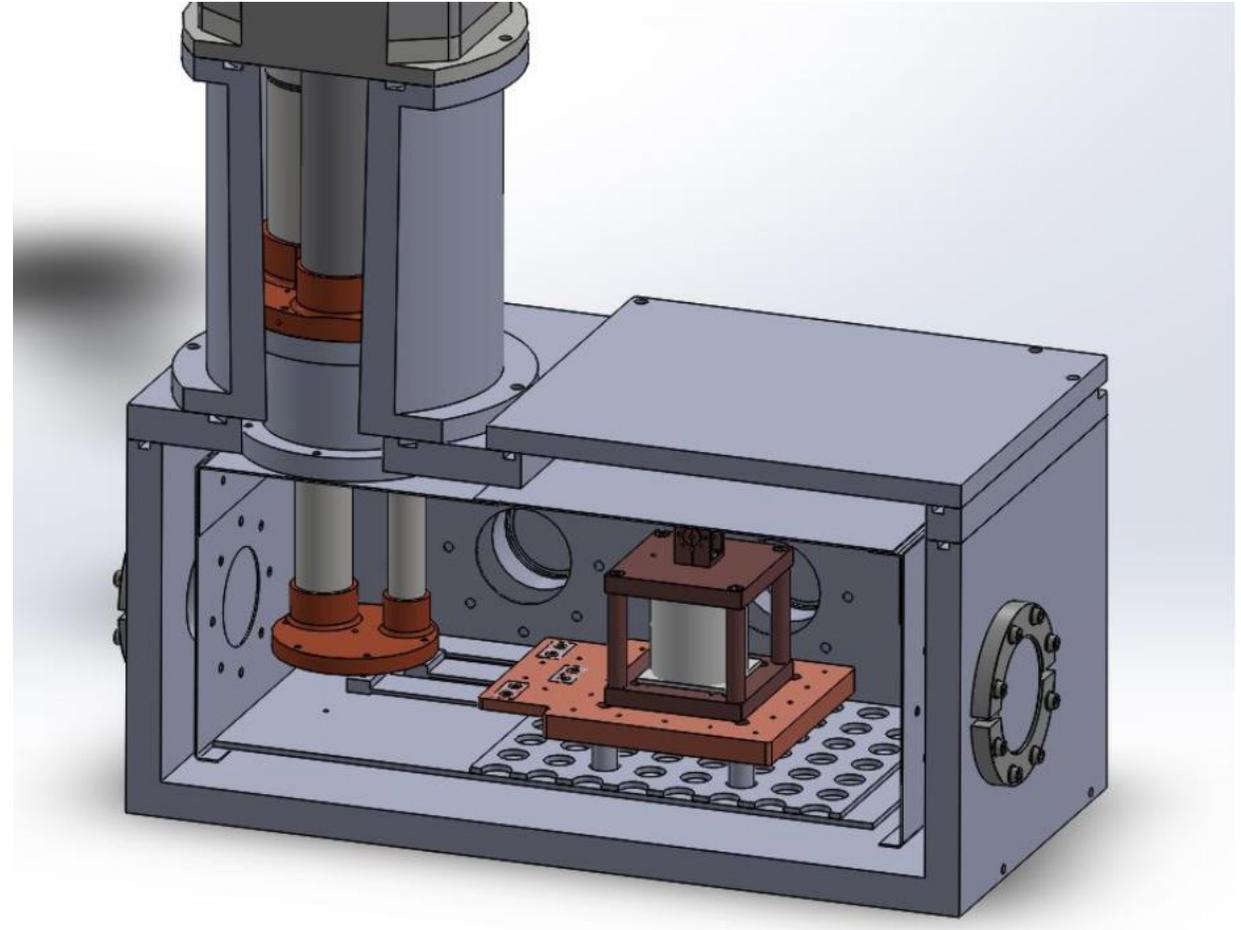


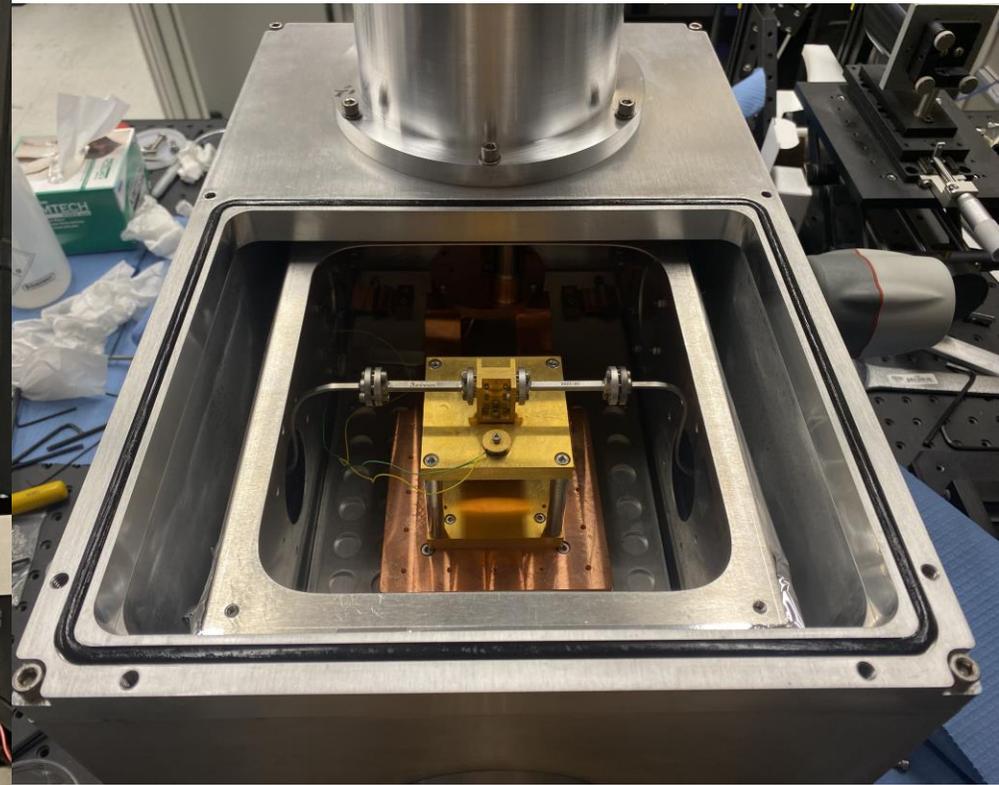
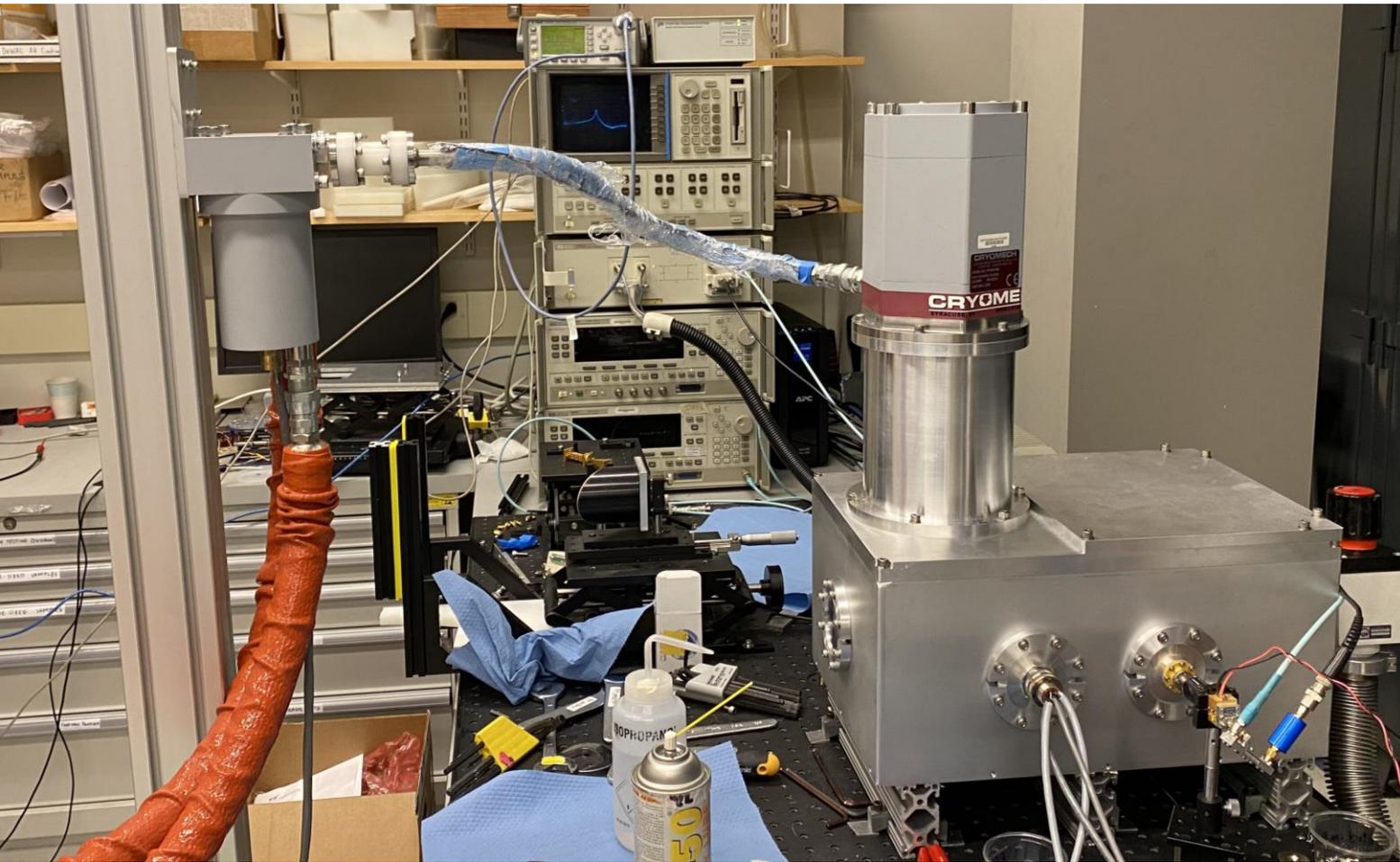
# Outline

- Context and motivation for using high-Q resonant cavities for measuring the complex permittivity of dielectrics
- Design and implementation of high-Q Fabry–Pérot resonators
- Measurement technique and results
- **Cryogenic measurements**
- What's on the horizon?

# A quick-turnaround cryostat

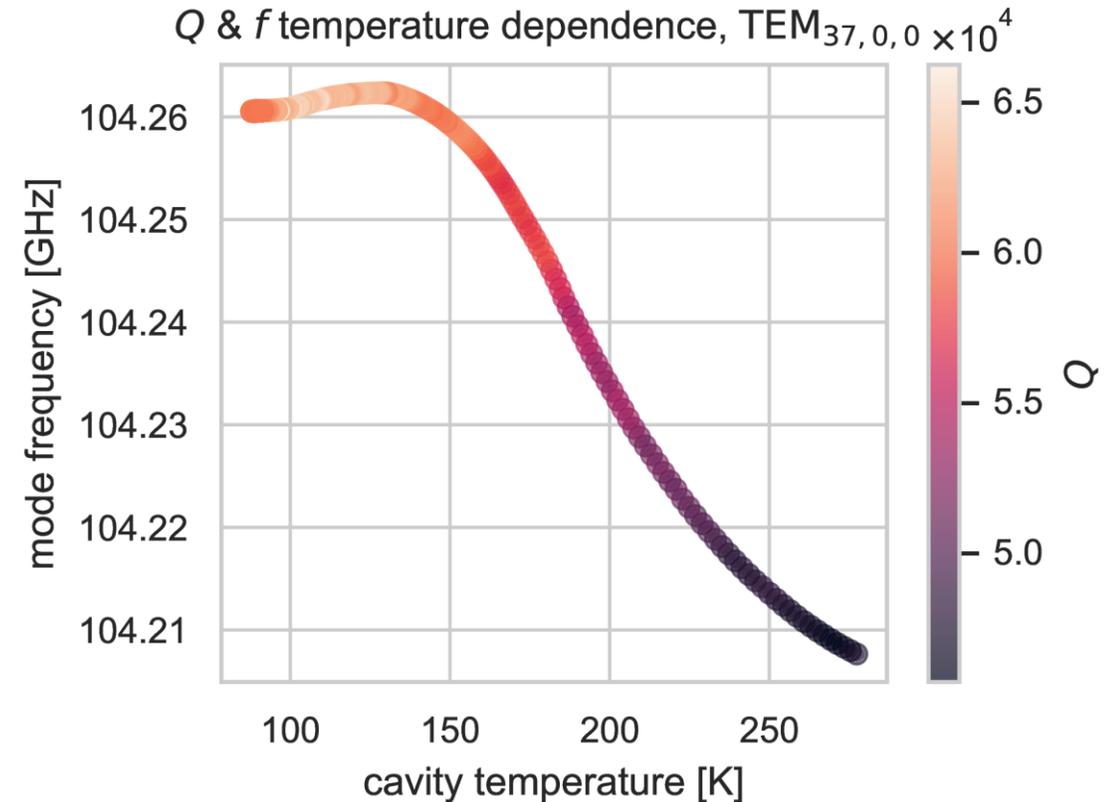
- A relatively compact cryostat that enables cooling the cavity and samples down to 4K.
  - Approx. 3-4-hour turnaround time
- Use an off-the-shelf PT405 pulse tube cryocooler to cool an active area and radiation shield.





# Empty cavity, cryogenic

- W-band cavity behaves as expected cryogenically.
  - Mode frequencies shift by amount expected by cavity length contraction.
  - In the first few cooldowns did not see issues from coupling-block induced distortions or worsening transmission leakage.
- Suspect improved mirror design will make cryogenic cavity more robust.



# Outline

- Context and motivation for using high-Q resonant cavities for measuring the complex permittivity of dielectrics
- Design and implementation of high-Q Fabry–Pérot resonators
- Measurement technique and results
- Cryogenic measurements
- **What's on the horizon?**
  - We are planning on a measurement campaign this spring, targeting room temperature W-band measurements.
  - Hope to compile and publish our measurement results in the near future!